

# Strong Lensing Legacy Survey

**Automated search for strong lenses in CFHTLS data**

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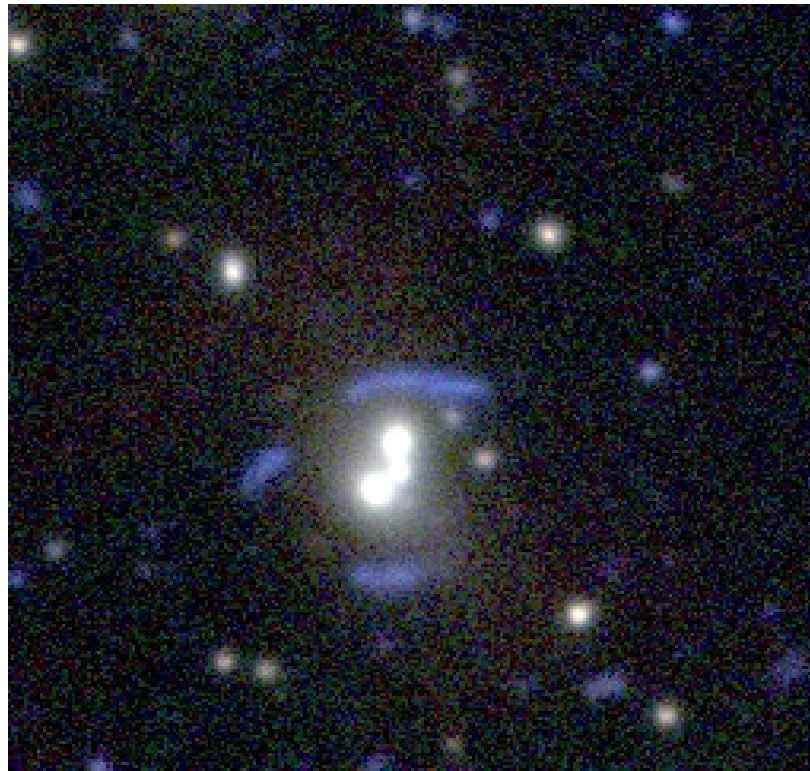
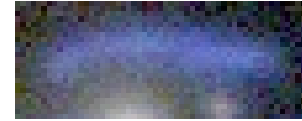
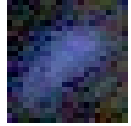
**Toulouse:** R. Cabanac (Tarbes), G. Soucail

**Marseille:** JP. Kneib

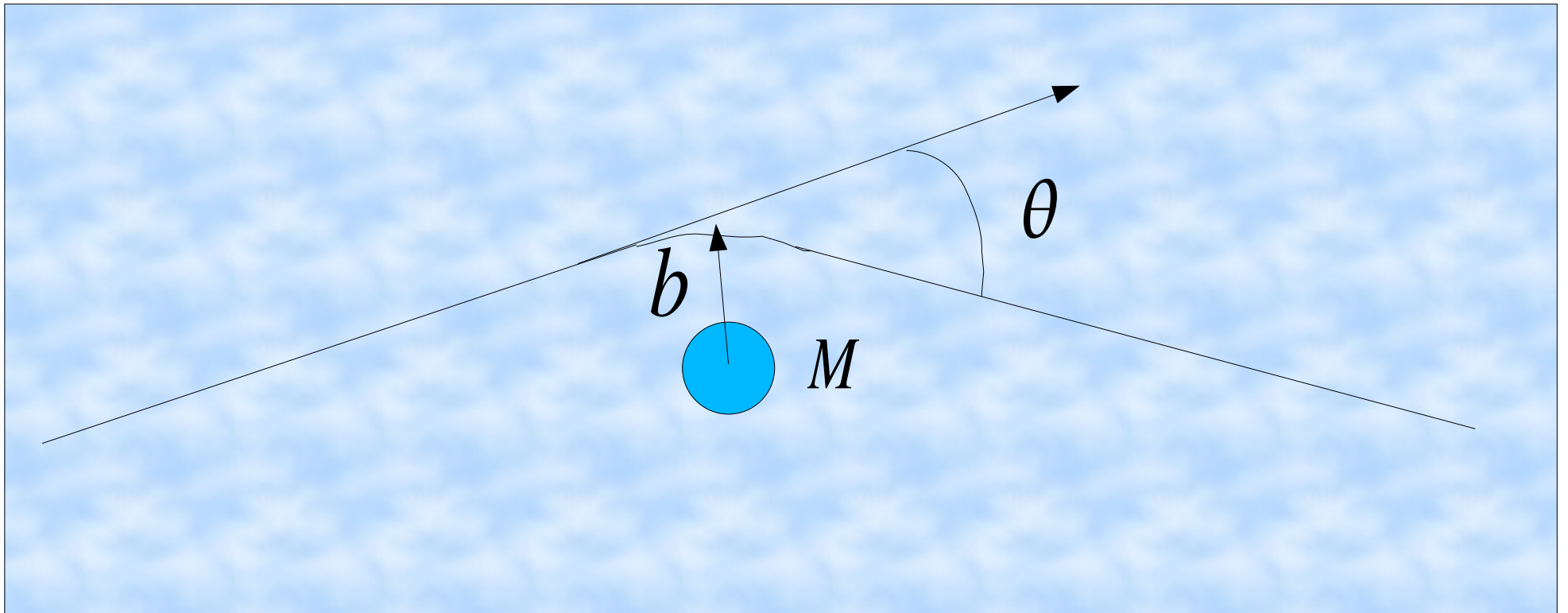
Abell 2218  
HST



**How to find highly distorted (arc-like) images, using automated softwares ?**



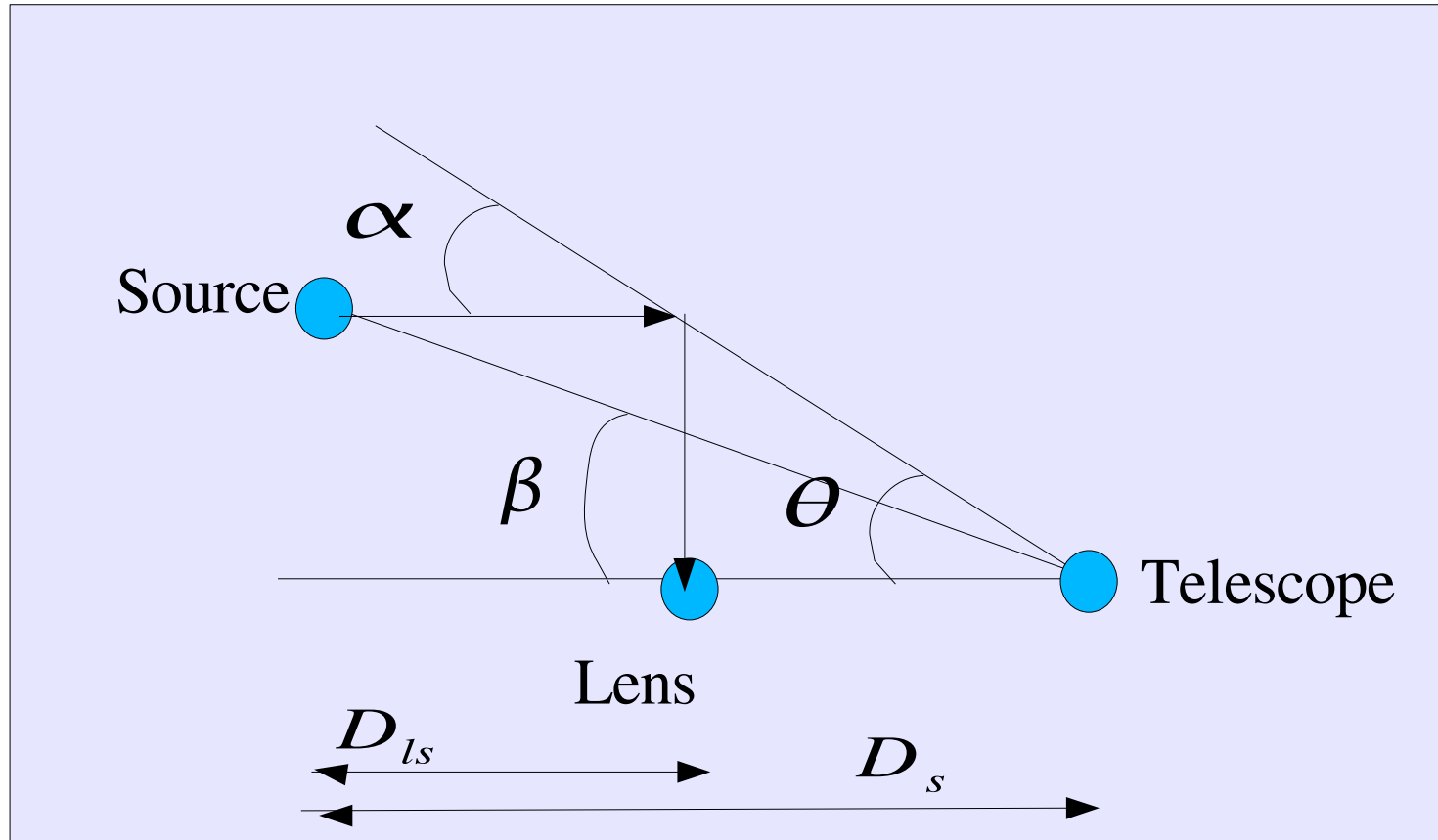
# Deflection par une masse



Relativite Generale au 1er Ordre

$$\theta = \frac{GM}{b}$$

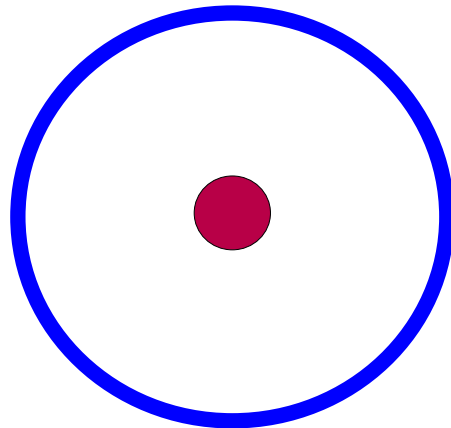
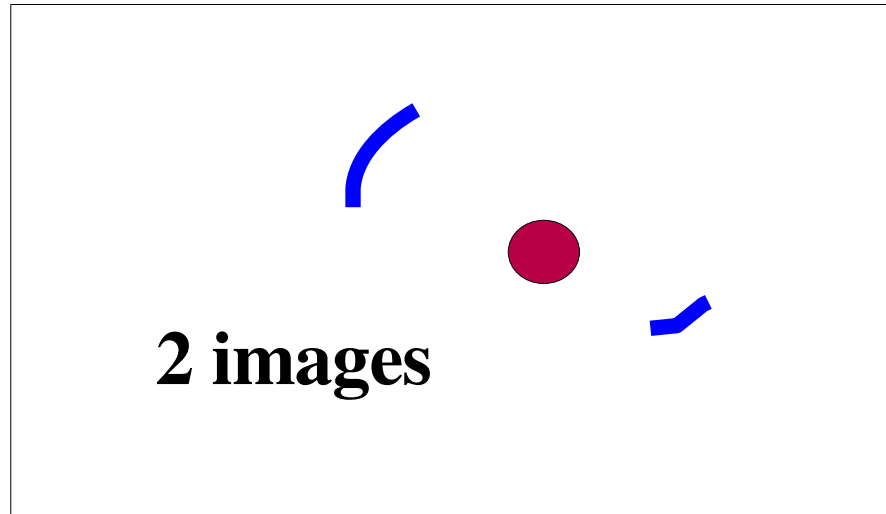
# Geometry of gravitational lensing



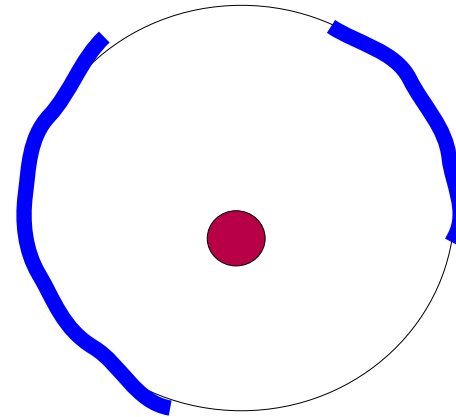
$$\beta = \theta - \frac{D_{ls}}{D_s} \alpha$$

**Lens equation**

# Lentille ponctuelle



**Alignement parfait**



**Leger desalignement**

# Spatially extended lens

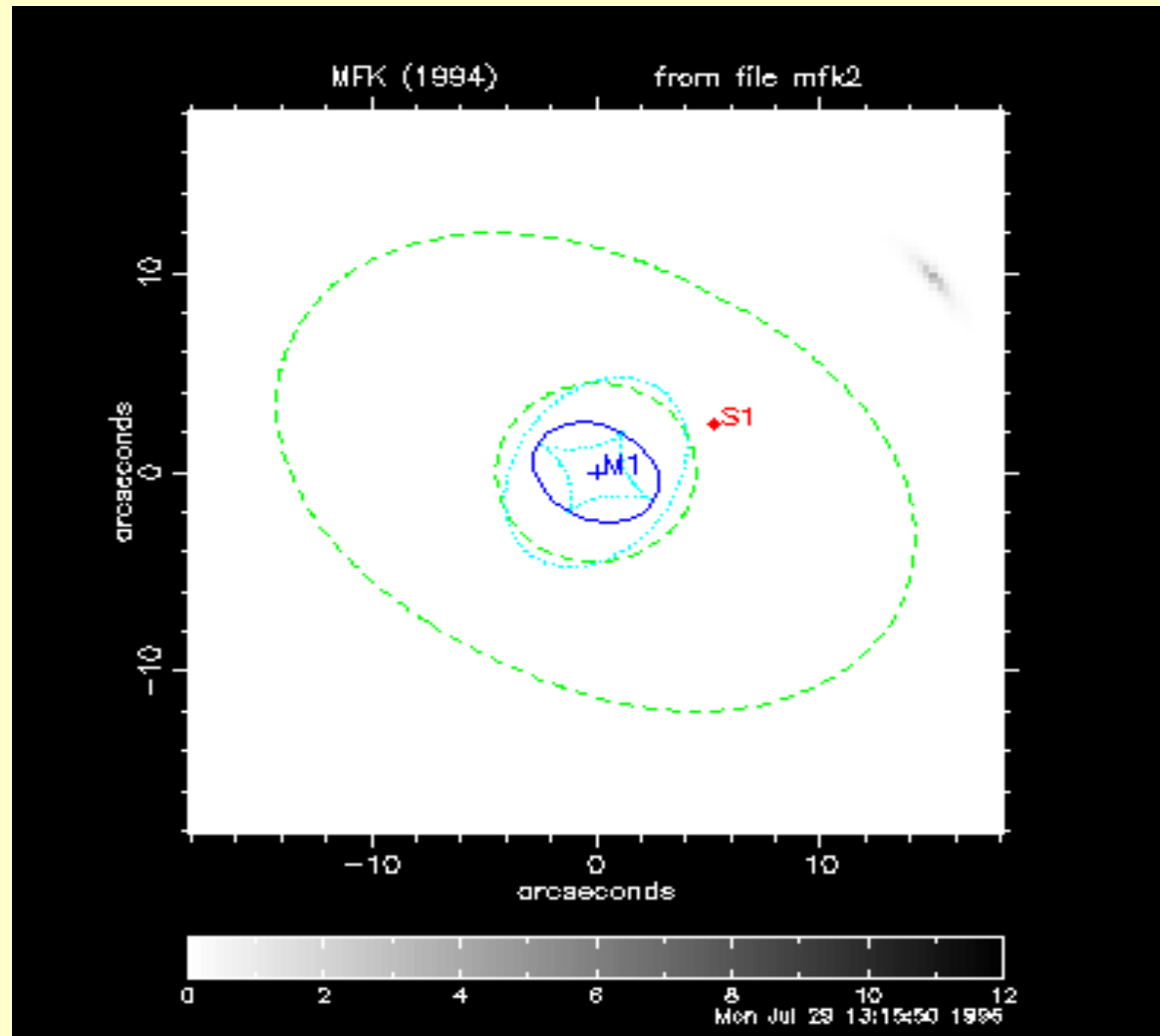
$$\beta = \theta - \frac{D_{ls}}{D_s} \alpha$$

**Lens equation**

$$\Delta \phi = 2 \rho$$

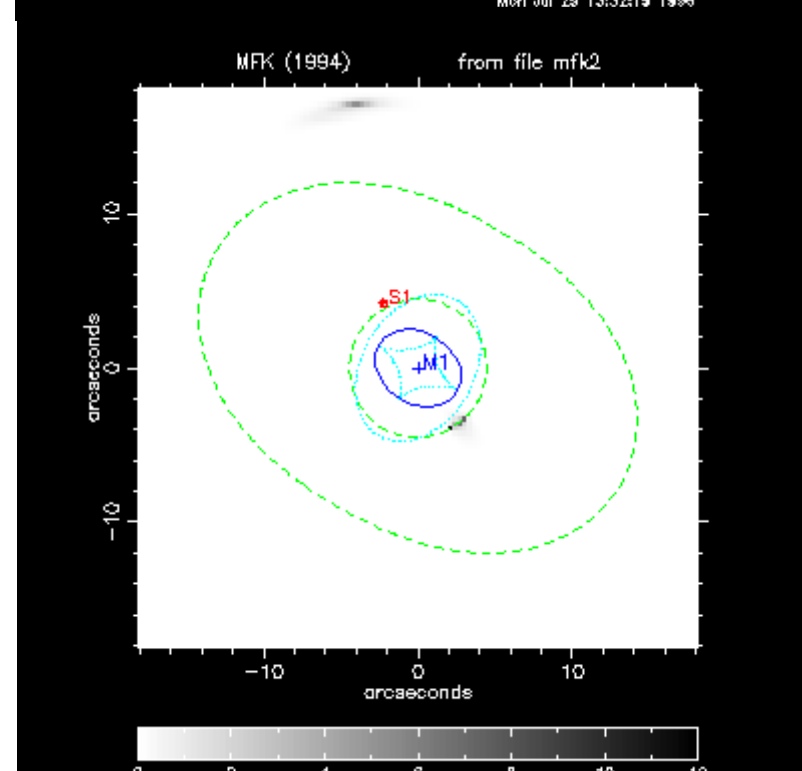
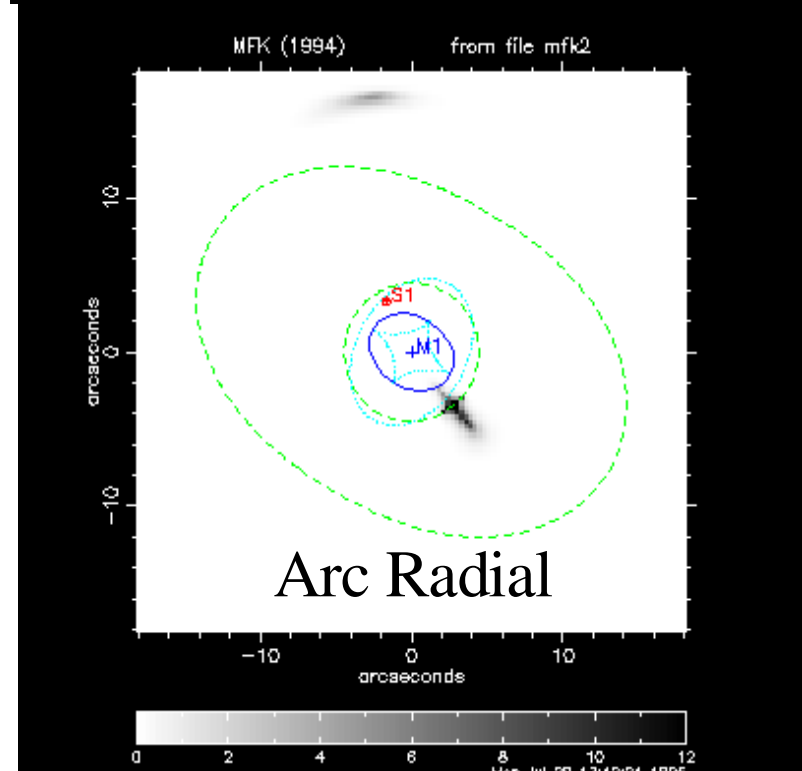
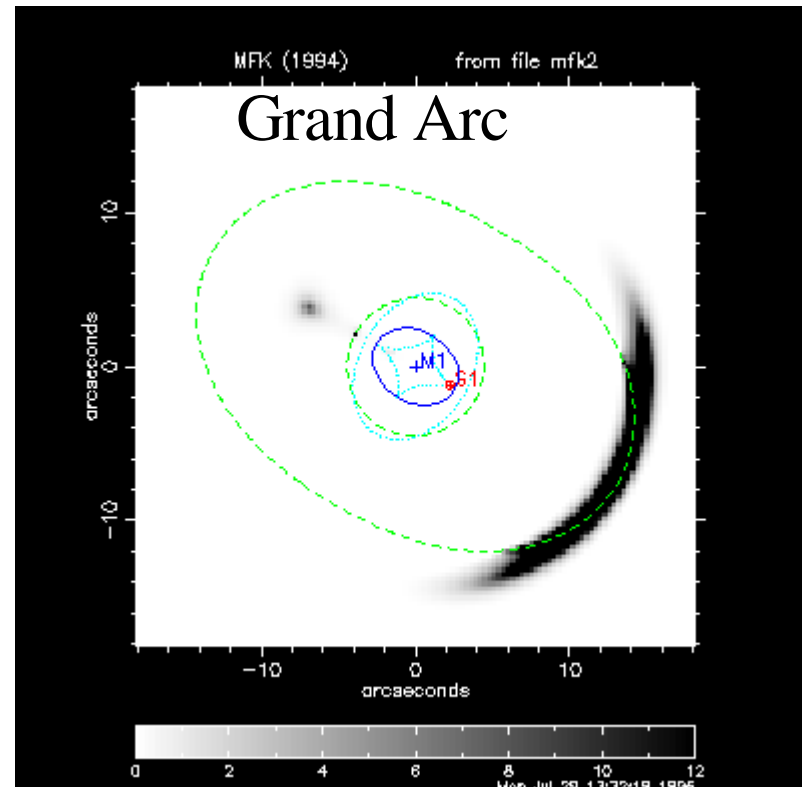
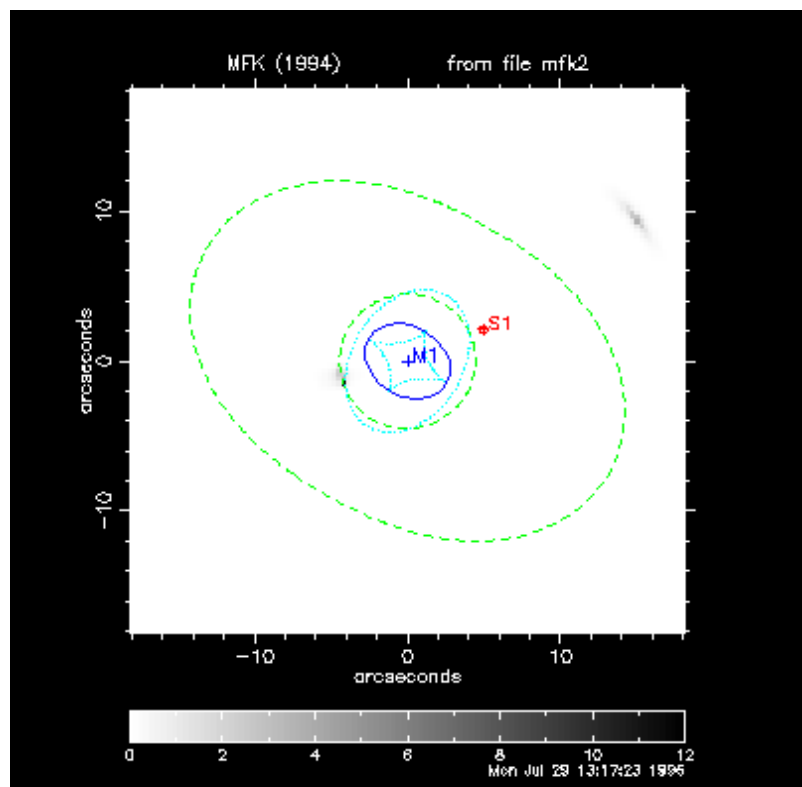
$$\alpha = \nabla \phi$$

# Elliptical lens with isothermal profile



Peter Newbury 1997



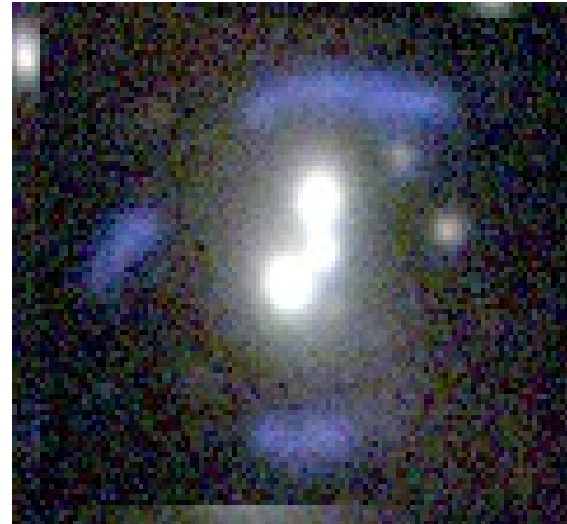


# Finding arcs or arclets in wide field CFHTLS images



**Most of the time**

**somewhat unusual**

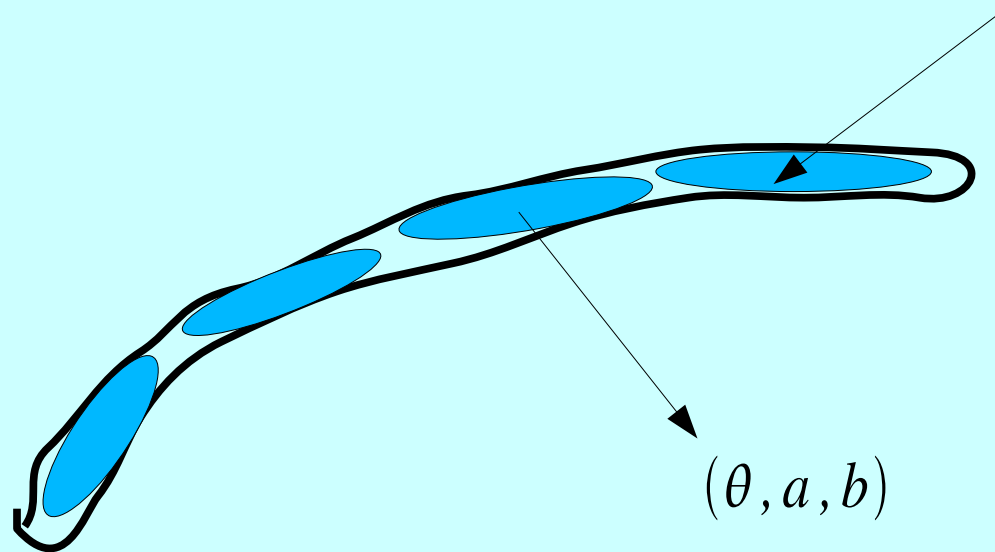


# Modeling arcs

Local decomposition of objects

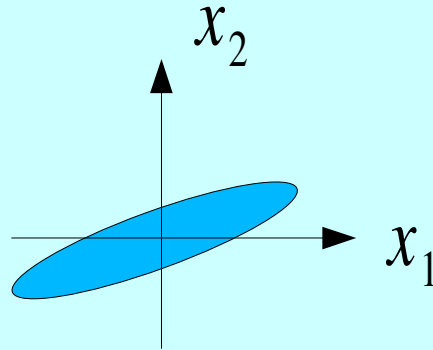
Tangent space

Metric



**local elongation and orientation at each point of the image**

# Estimating local geometry



2<sup>nd</sup> order Moments  $\sigma_{ij} = \int I(x_1, x_2) x_i x_j dx_1 dx_2$

Rotation, in proper axis:  $\sigma_{12} = 0$

Local elongation, ratio of 2<sup>nd</sup> order moments:  $\frac{\hat{\sigma}_{11}}{\hat{\sigma}_{22}}$

## Parameters of local geometry

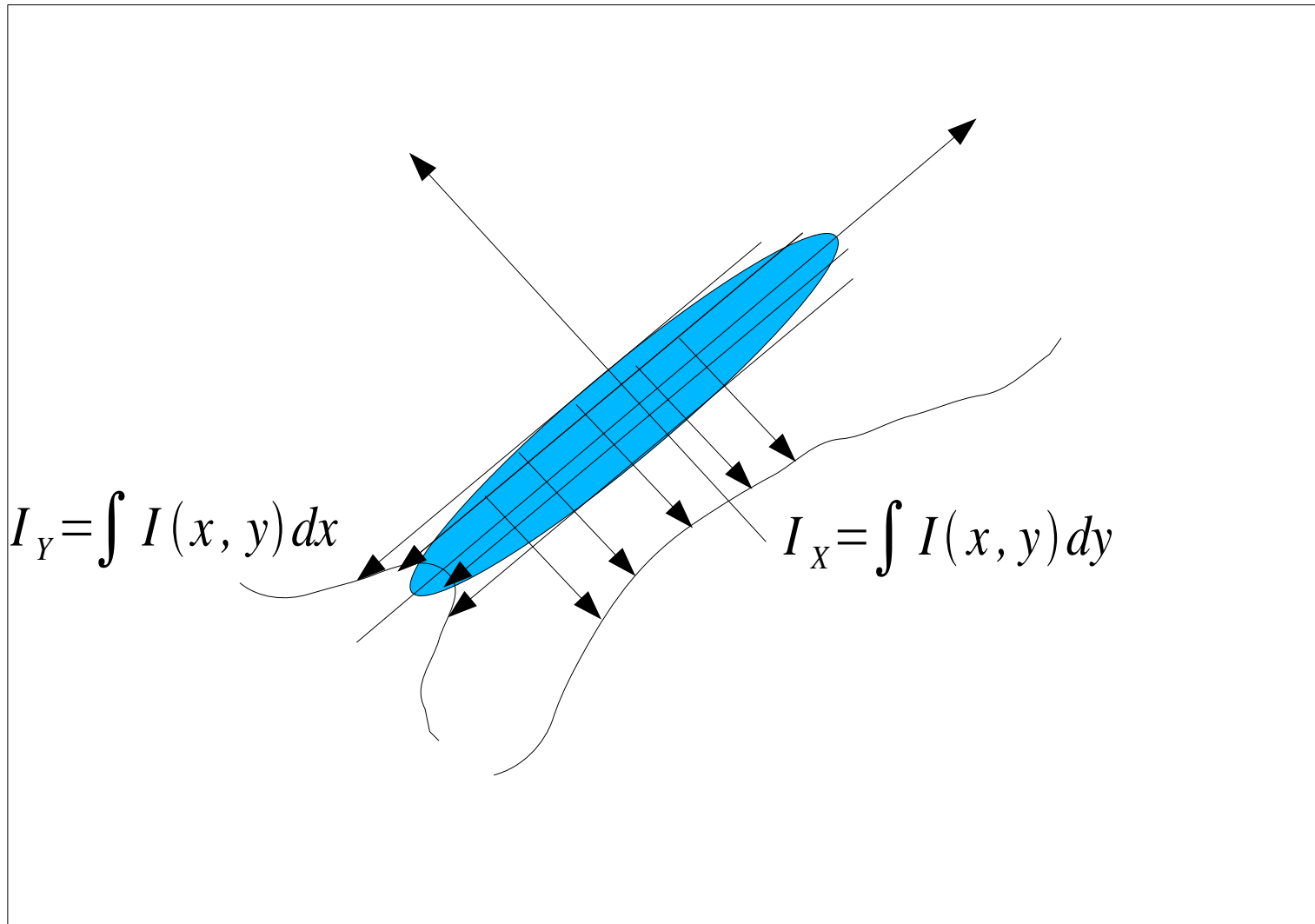
Estimation of  $\theta$  not very noisy using 2<sup>nd</sup> order moment

Variance on  $\theta$  proportional to noise variance

$$\sigma_{\theta} \simeq \frac{1}{4} \frac{S}{N} \simeq 1^{\circ} \text{ for } \frac{S}{N} = 10$$

Elongation a:b --> divergent, very sensitive to noise  
and to details of the local distribution

# Estimating local elongation



**Marginal Distributions projected along axis**

# Elongation estimator

$$Q(x_0, y_0) = \frac{1}{2M} \frac{I_Y(x_0)}{\text{SUP.}[I_X(x_0+x)]_{[-M < x < M]}}$$

*Decomposable locally*  $I(x+x_0, y+y_0) = f(x)g(y)$

$$Q(x_0, y_0) \leq \frac{g(0)}{\int g(y) dy} \quad g(y) = \alpha G\left(\frac{y}{b}\right) \quad Q(x_0, y_0) \leq \frac{G(0)}{b}$$

Bounded estimator, maximal for small b (PSF size)

Equal to sup bound if distribution is flat along main axis ~ Arc

## Other propriety of the estimator

Homothetic profiles:  $f(x) = \alpha F\left(\frac{x}{a}\right)$  ;  $g(x) = \beta G\left(\frac{x}{b}\right)$

$$(a, b) \ll M, Q(x_0, y_0) = \frac{G(0)}{2M} \frac{a}{b}$$

$$a \gg M, Q(x_0, y_0) \rightarrow \frac{G(0)}{b} \quad \text{Saturation value}$$



## Noise on estimation of local elongation

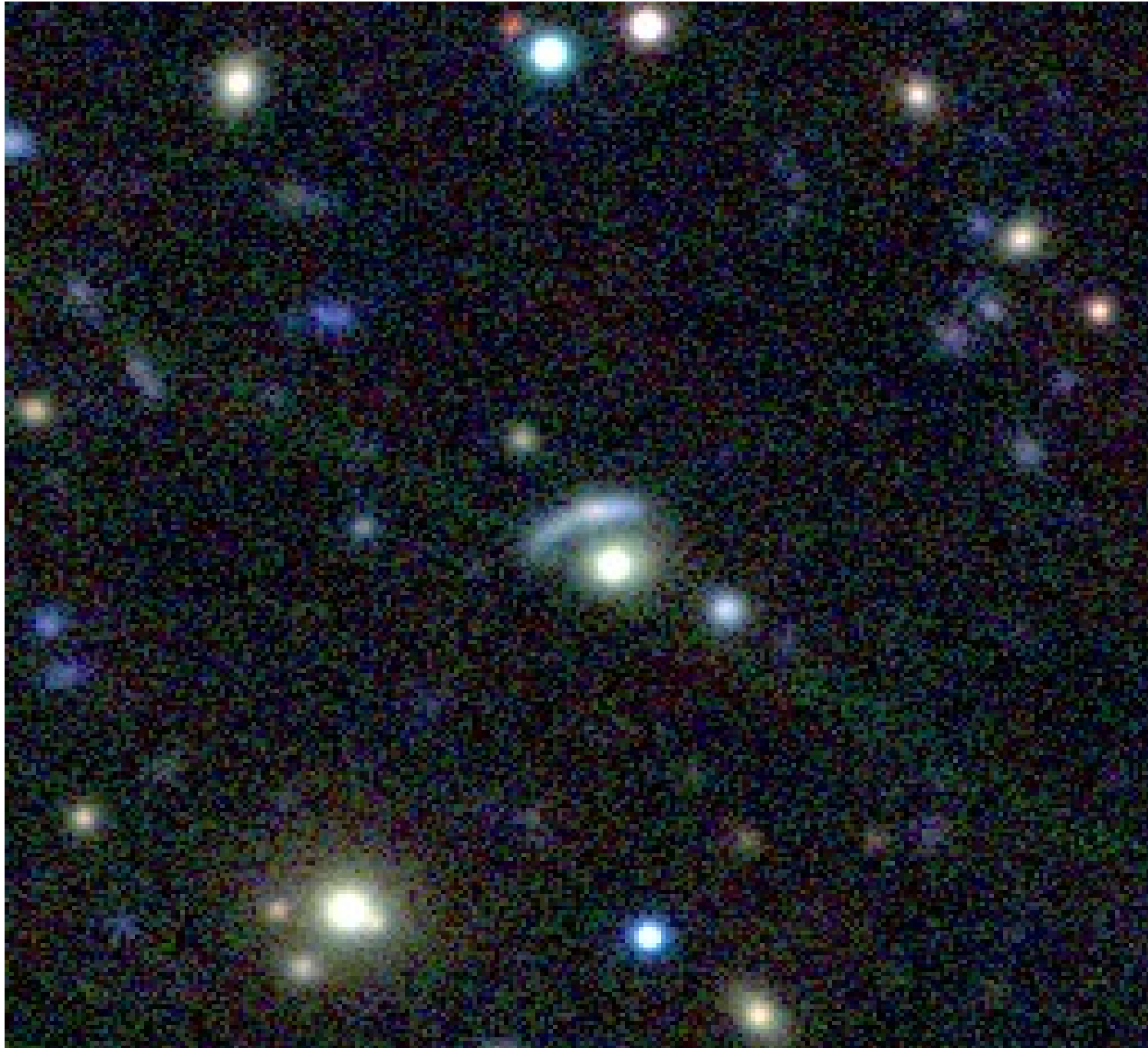
Truncated expansion of  $Q(x,y)$  for small errors  
Combination of errors for the 2 marginals distribution  
using an order statistics

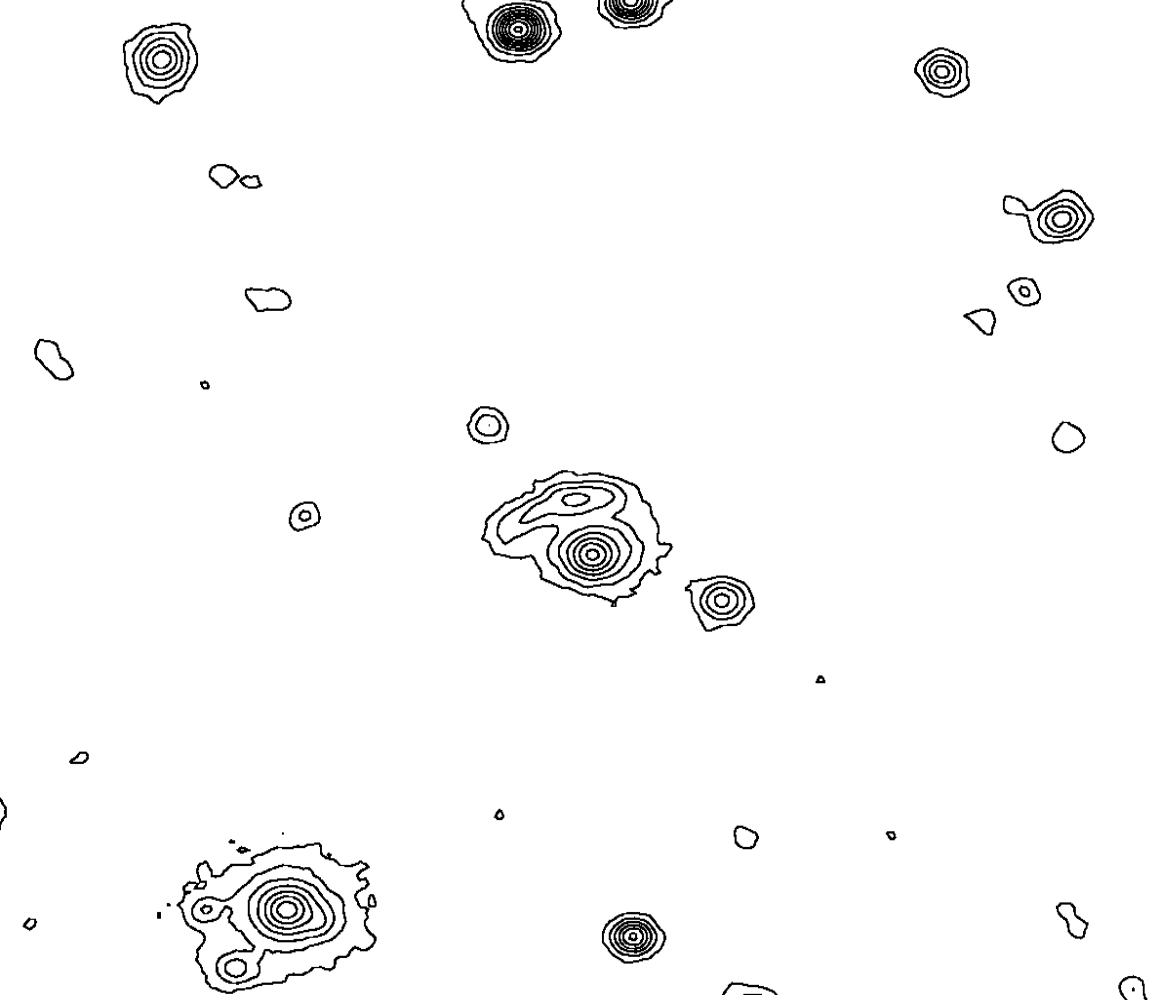
$$\frac{Q}{N_\varrho} \simeq 0.45 \frac{S}{N}$$

For  $\frac{S}{N} = 10$  noise is only  $\sim 20\%$  of signal

Dynamic on  $Q(x,y) \sim$  factor 3, noise is not an issue

# Illustration with CFHTLS wide image





CFHTLS image

Calculation of local estimator  
at each point



Small arcs – observational  
limits



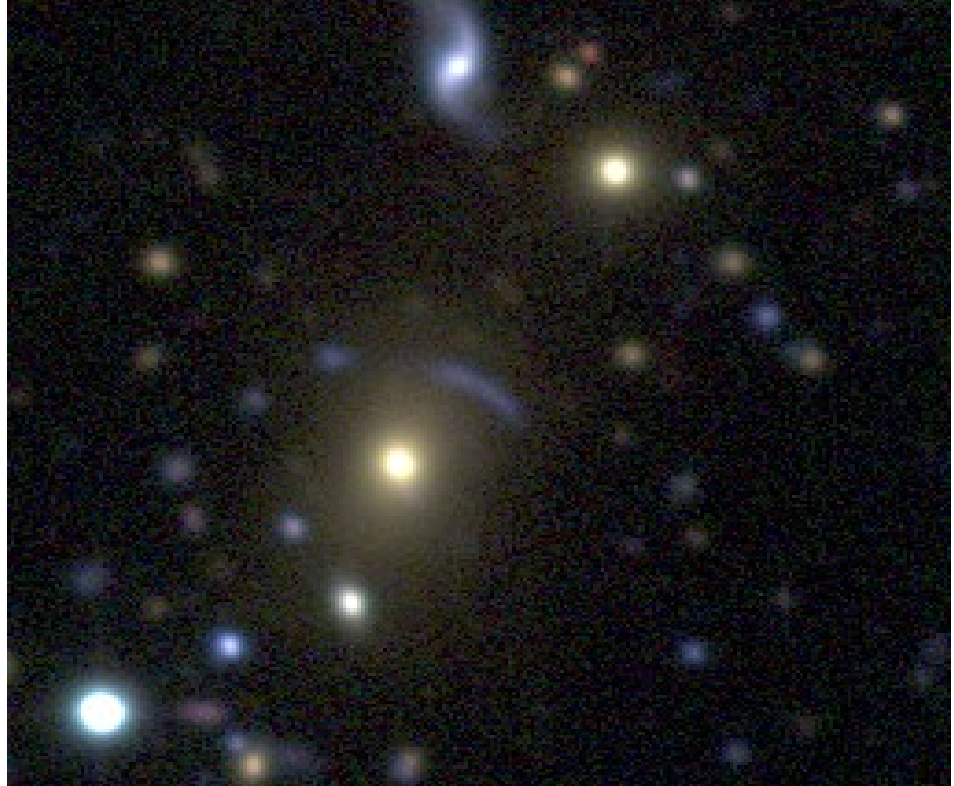
## Galaxy groups

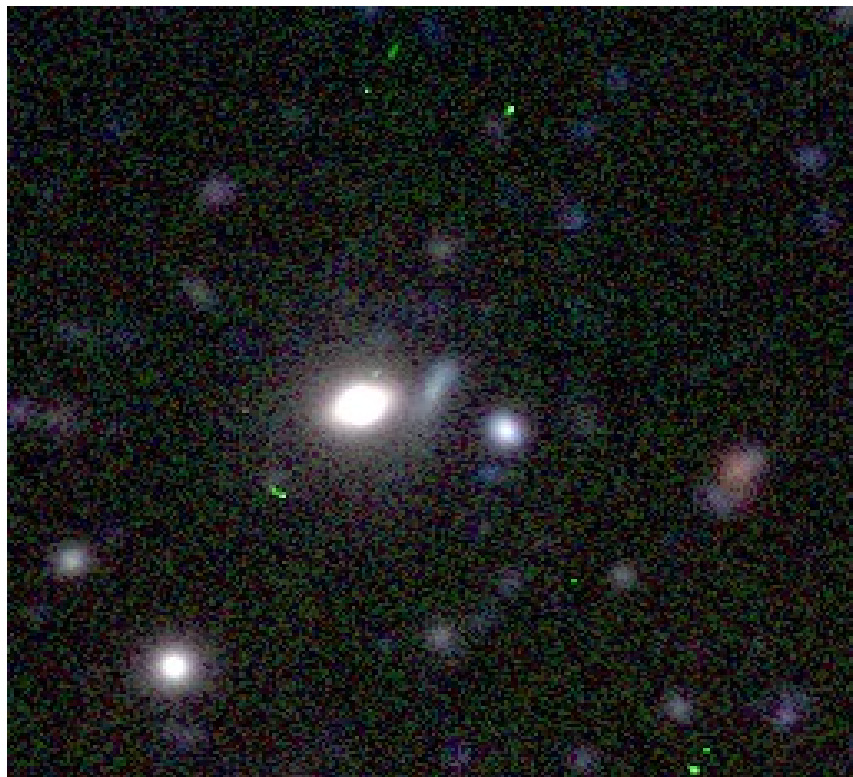
Typically a few tens of galaxies

Mass  $\sim 10^{13}$  Solar mass

Velocity dispersion inside group  
a few hundreds km/s

Lensing due to galaxy groups, separations  
of a few arc seconds

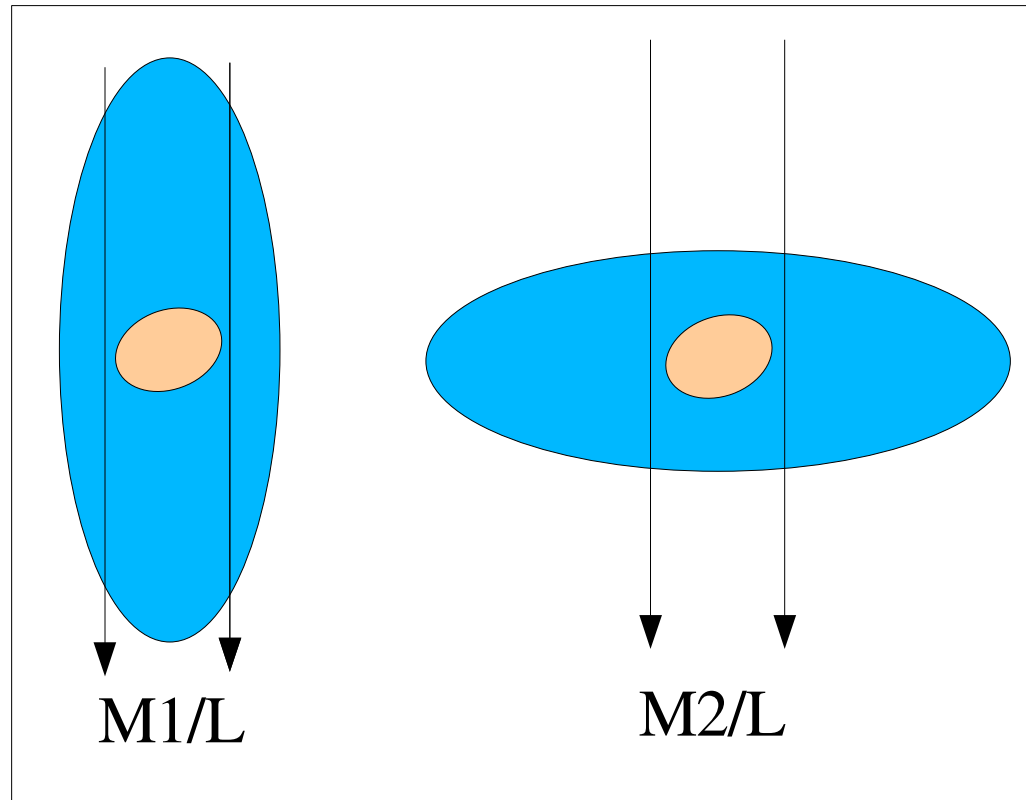




Arcs appears near critical radius  
size of system is close to Einstein radius  
-----> Estimation of Einstein radius  
-----> Mass of deflector

Ellipticity of halos

$$M1/L > M2/L$$





Effect of sub-structures, small perturbations  
of caustics --> arc shape modified  
col dark matter granularity, visible  
in arcs ?

Uneasy to disentangle  
from intrinsic source  
granularity



## Future

Data acquisition & data reduction

Spectro & redshifts: ESO Proposals, Gemini

Automated search in new CFTHLS releases

Comparison of the observational search with  
cosmological models – Ray tracing in numerical  
simulations, reconstruction of arcs, computation  
of arcs properties & estimation of detection efficiency

on numerical simulations