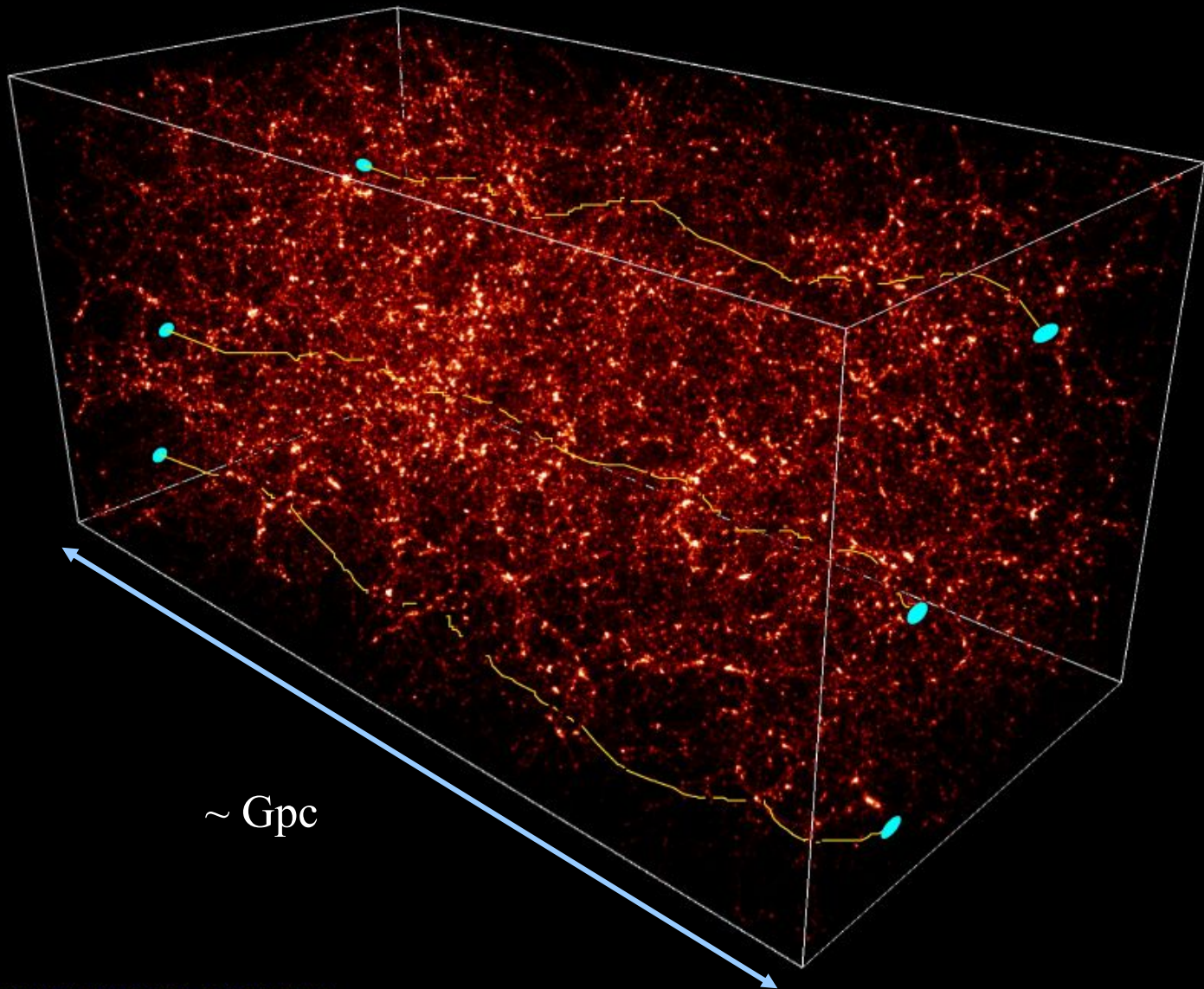


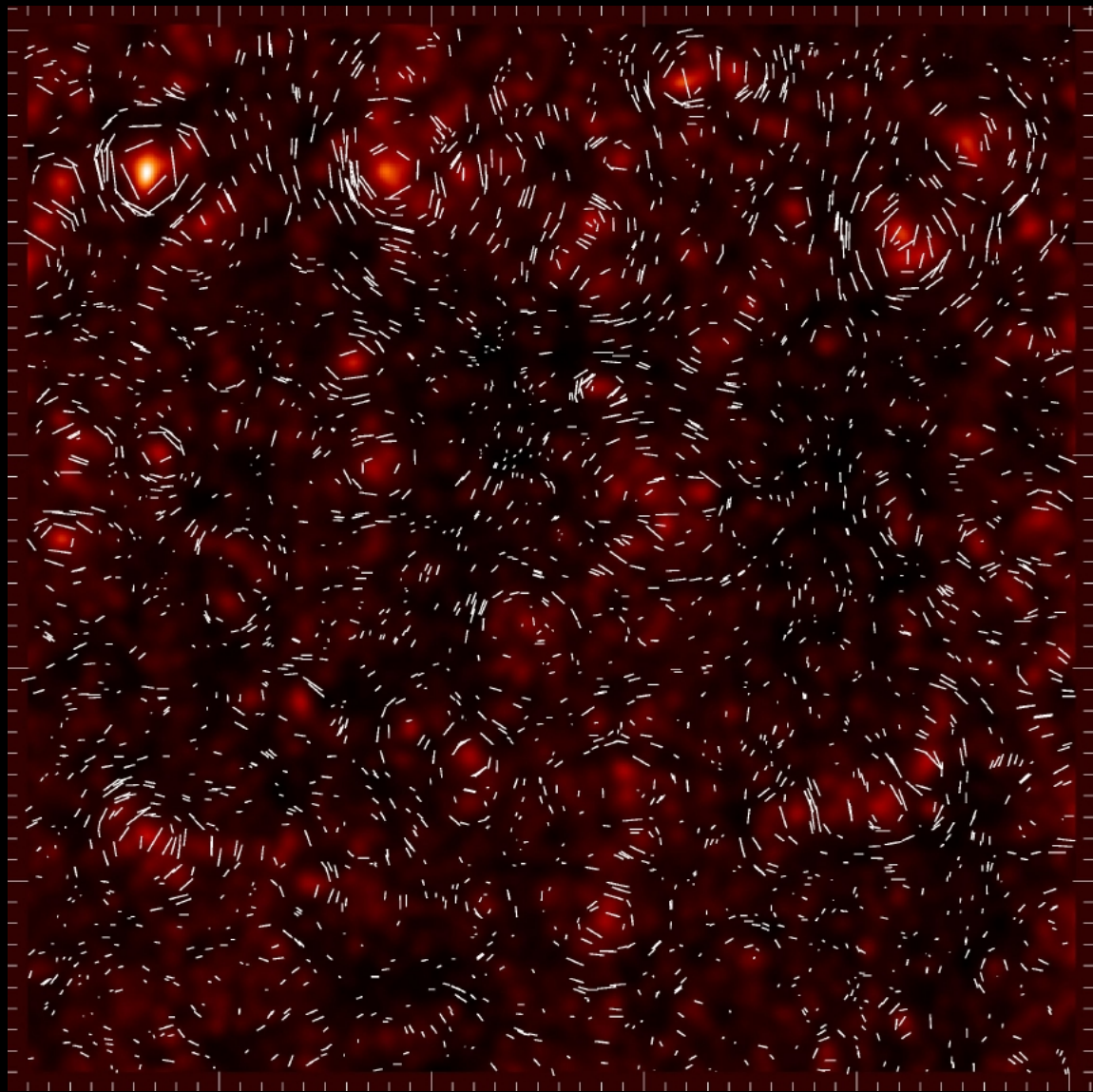
Cosmic Shear and WIRCAM

Mellier, van Waerbeke, Bertin, Tereno, Bernardeau, et al.

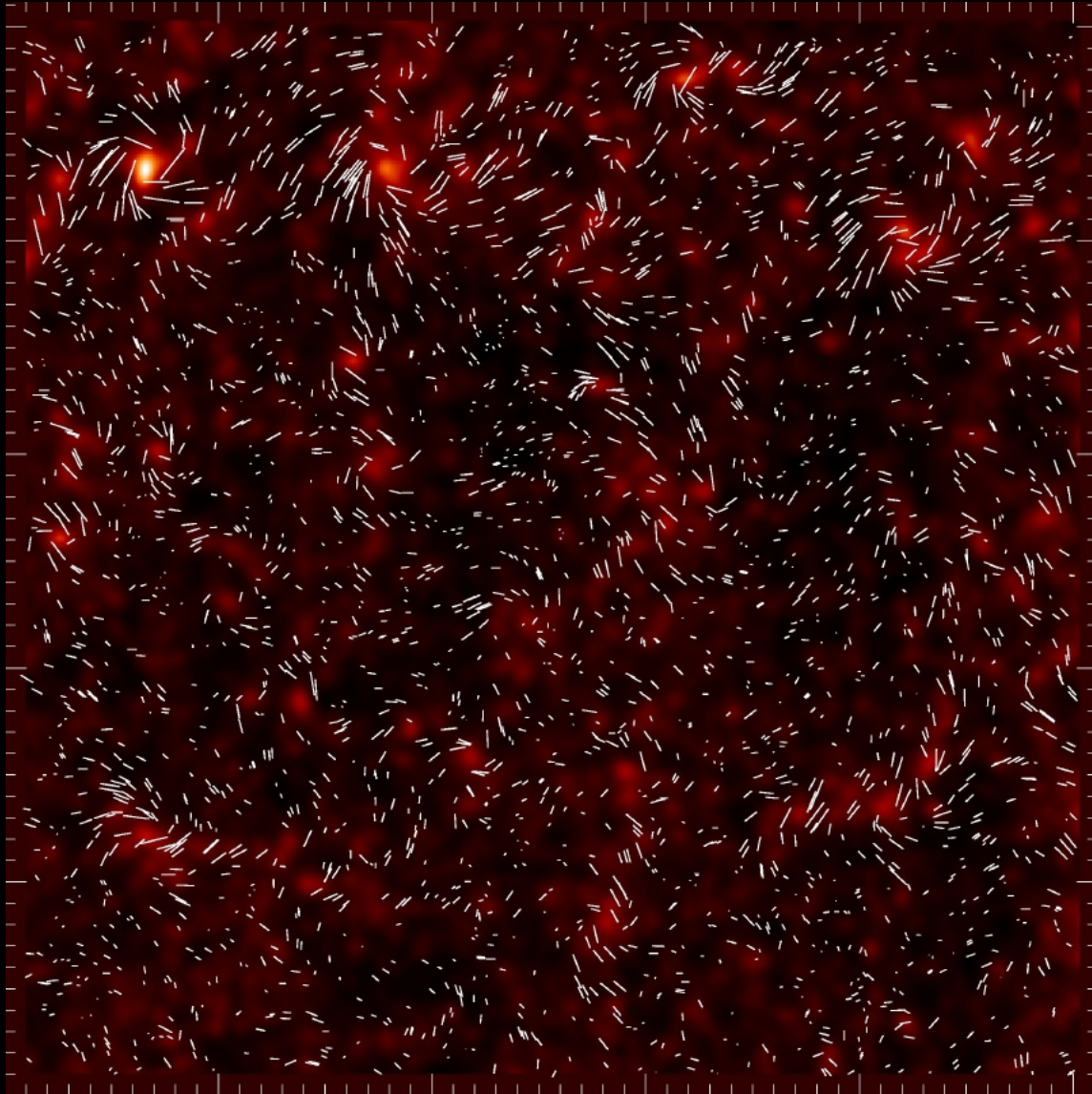
WIRCAM Workshop on LPs
November 5-6 , 2004

DEFLECTION OF LIGHT RAYS CROSSING THE UNIVERSE, EMITTED BY DISTANT GALAXIES





45 degrees rotated
galaxies, E \rightarrow B



Gravitational lensing does not produce B-modes:

Dark matter properties with cosmic shear

(Blandford et al 1991, Miralda-Escudé 1991, Kaiser 1992, 1998, Bernardeau et al 1997, Jain & Seljak 1997, Schneider et al 1998)

Top-hat shear variance at scale θ_c :

$$\langle \gamma^2 \rangle = \frac{2}{\pi \theta_c^2} \int_0^\infty \frac{dk}{k} P_\kappa(k) [J_1(k\theta_c)]^2$$

Aperture mass (M_{ap}) variance at scale θ_c :

$$\langle M_{ap}^2 \rangle = \frac{288}{\pi \theta_c^4} \int_0^\infty \frac{dk}{k^3} P_\kappa(k) [J_4(k\theta_c)]^2$$

Shear correlation function at separation θ :

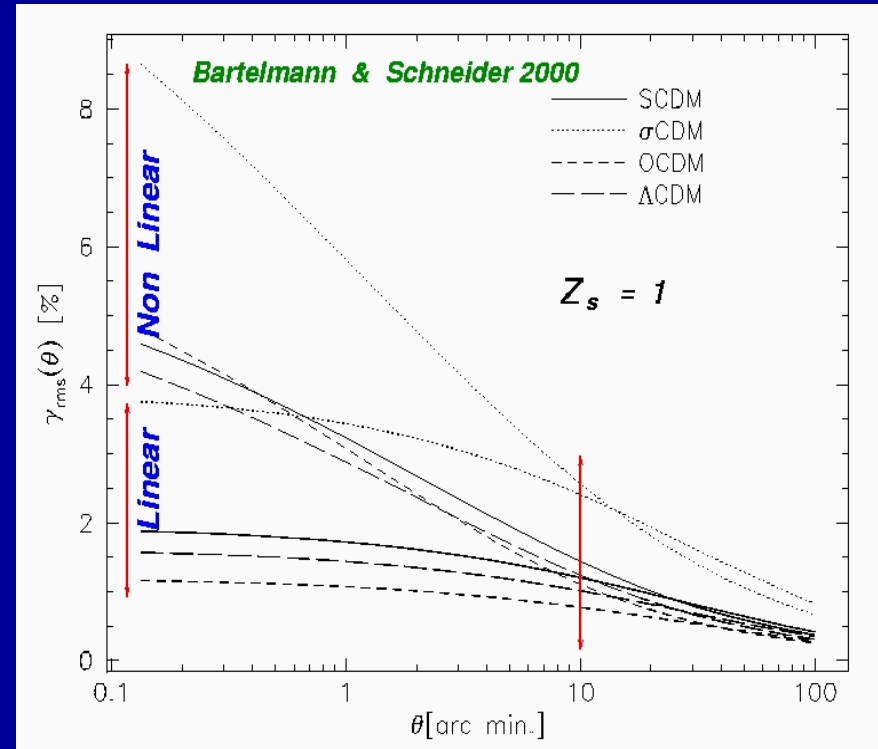
$$\langle \gamma(r) \gamma(r+\theta) \rangle_r = \frac{1}{2\pi} \int_0^\infty dk k P_\kappa(k) J_0(k\theta)$$

Convergence (projected mass) power spectrum:

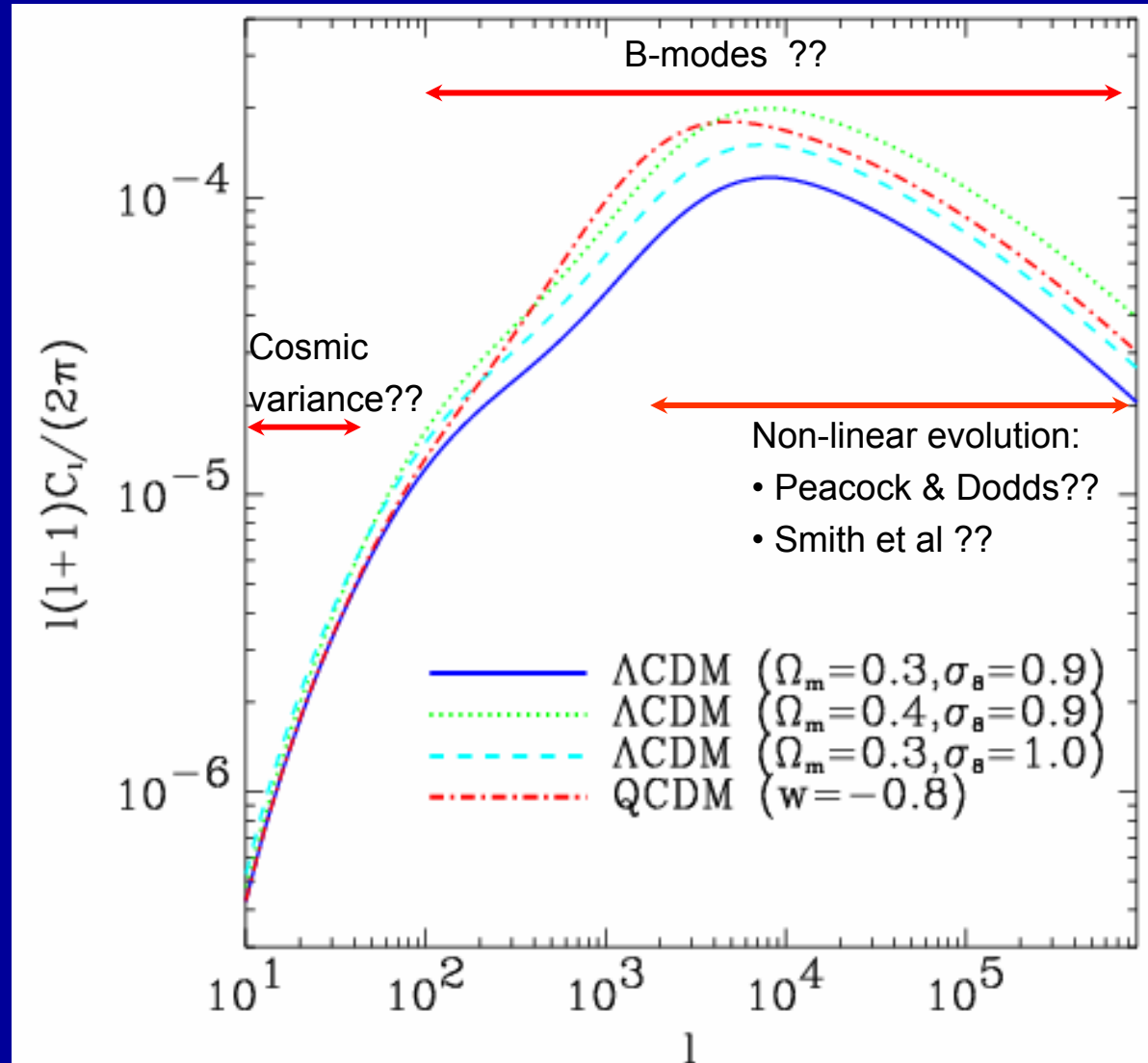
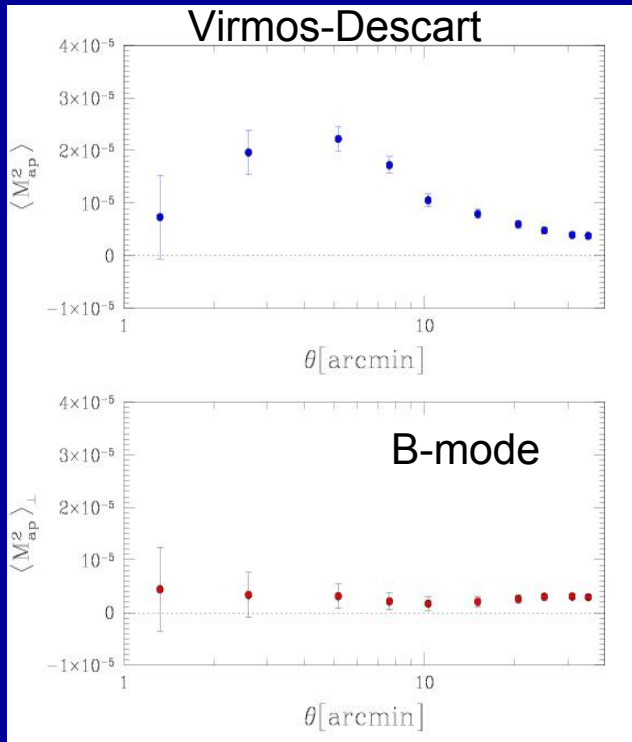
$$P_\kappa(k) = \frac{9}{4} \Omega_0^2 \int_0^\infty dz \cdot P_{3D}\left(\frac{k}{D_L(z)}; z\right) \cdot F[z, z_{source}]^2$$

Assuming a single lens-plane and $P(k) \propto k^n$:

- $\langle \kappa^2(\theta) \rangle^{1/2} \approx 0.01 \sigma_8 \Omega^{0.8} \left(\frac{\theta}{\text{Iddeg.}}\right)^{-\frac{n+2}{2}} z_s^{0.75}$
- $\langle \kappa^2(\theta) \rangle = \langle \gamma^2(\theta) \rangle$



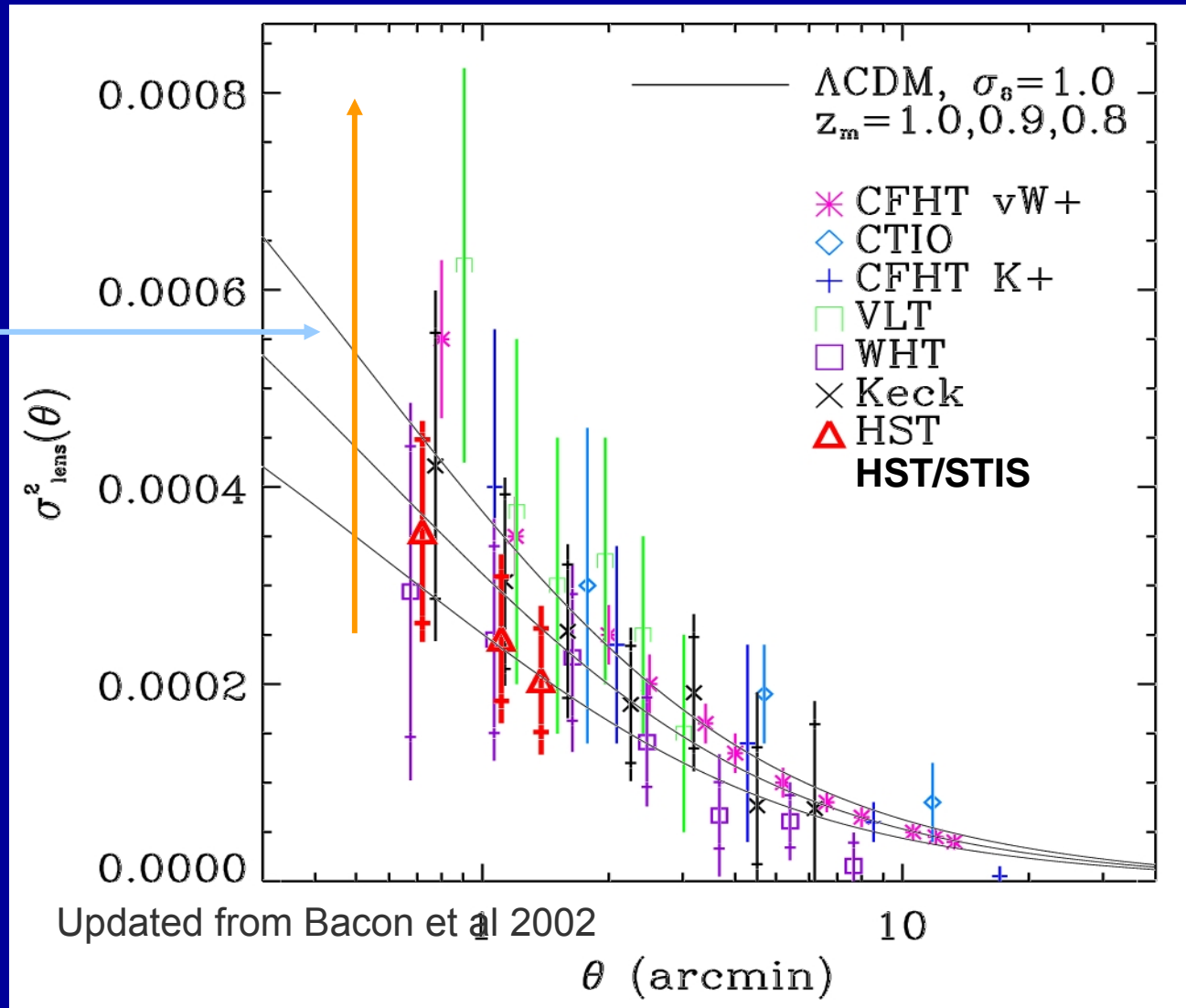
Cosmic shear surveys and dark energy: the goal is $P(k)$ and $P(k,z)$



Cosmic shear surveys: $\langle \gamma^2 \rangle$ Consistency between the teams

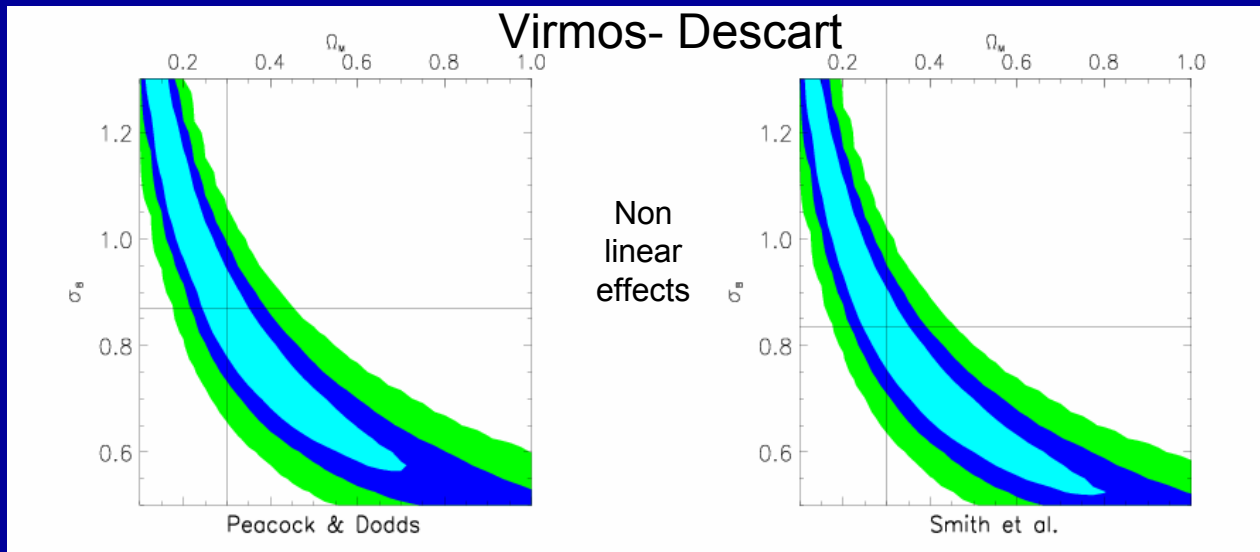
Theoretical expectations:
CDM + gravitational
instability paradigm

- More than 150 deg²
- More than 200 uncorelated fields
- $0.1 < z_s < 1.2$
- More than 11 instruments
- 3 Space, rest from ground

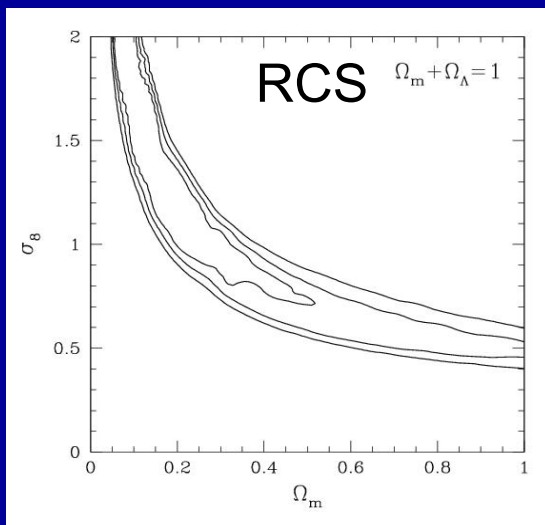


Van Waerbeke et al 2000, 2001, 2002, 2004; Wittman et al 2000; Bacon et al 2000, 2003; Kaiser et al 2000; Maoli et al 2001; Réfrégier et al 2002; Hoekstra et al 2002, Haemmerle et al 2001, Rhodes et al 2001, 2004, Brown et al 2002, Hamana et al 2002, Jarvis et al 2002, Massey et al 2004.

Virmos- Descart



van Waerbeke, Mellier, Hoekstra 2004

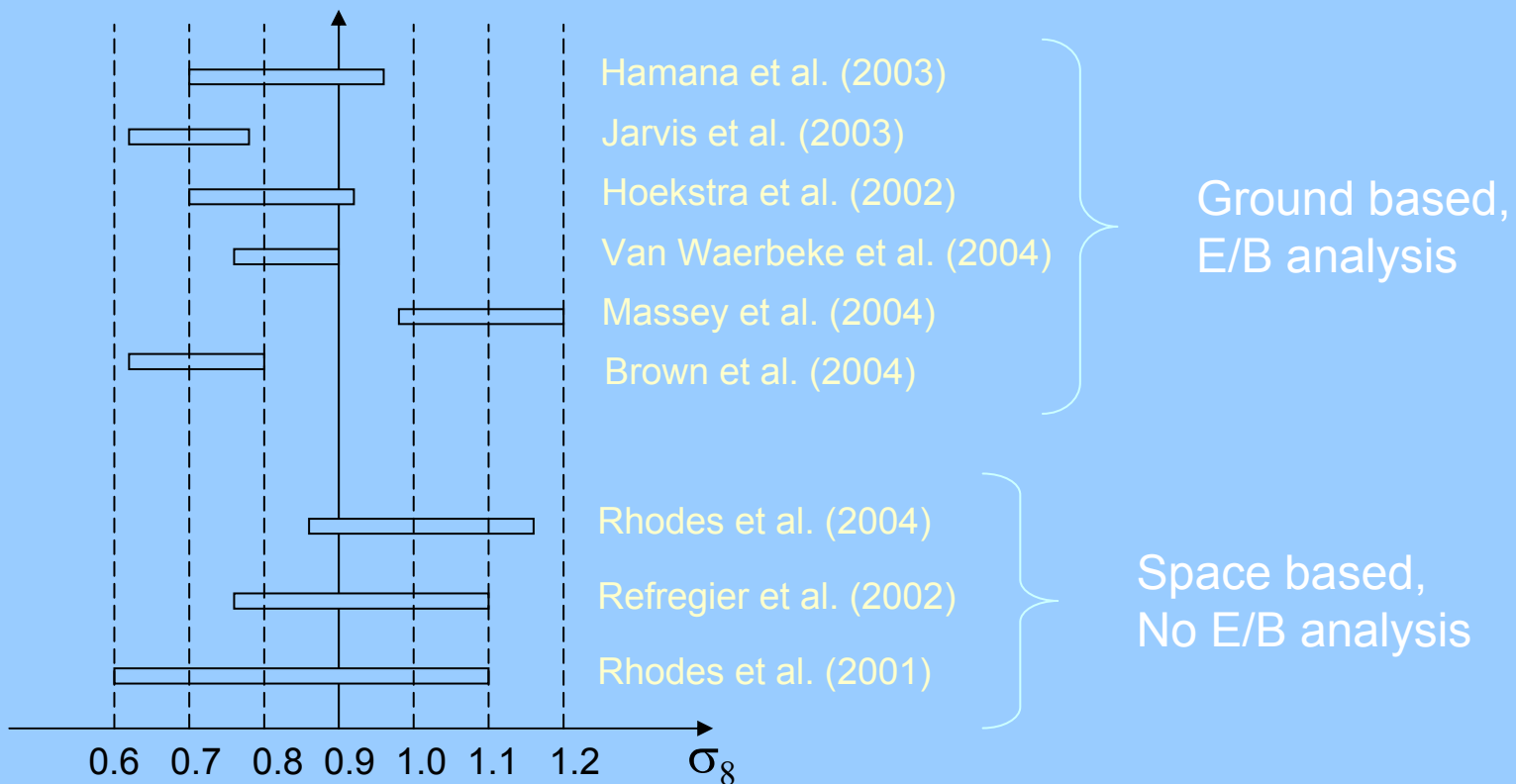


Hoekstra, Yee, Gladders, 2002

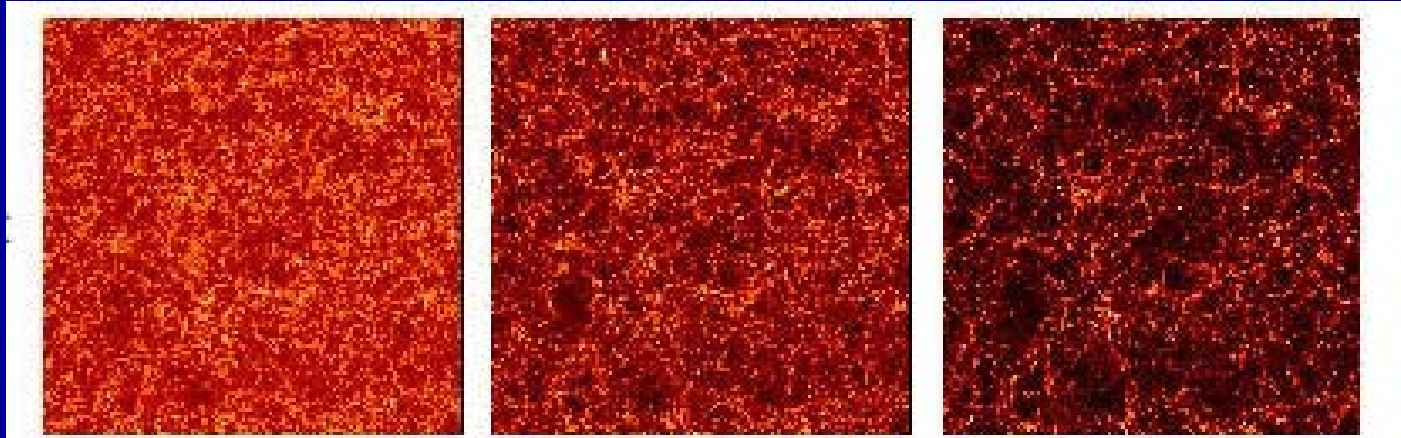
Virmos-Descart + RCS:
 $\Omega_m = 0.30 \pm 0.10$
 $\sigma_8 = 0.85 \pm 0.10$ (99.5%)

Summary of the most recent results

1σ measures of σ_8 for the ground E/B analysis and for all space based observations.



Ω_m - σ_8 degeneracy with higher order statistics: Skewness of the convergence



Assuming a single lens-plane and $P(k) \propto k^n$:

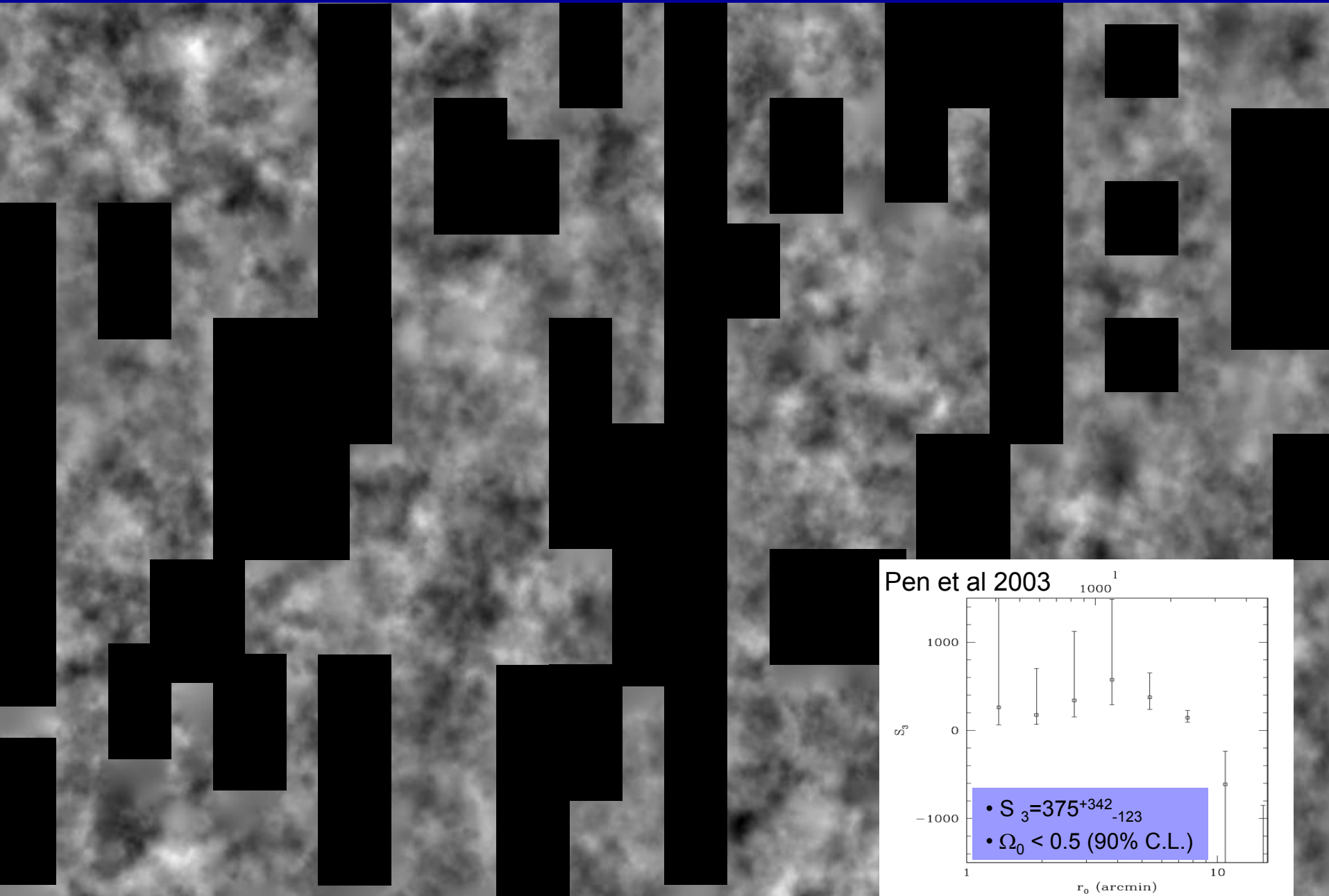
$$\bullet \langle \kappa^2(\theta) \rangle^{1/2} \approx 0.01 \sigma_8 \Omega^{0.8} \left(\frac{\theta}{1 \text{ deg.}} \right)^{-\frac{n+2}{2}} z_s^{0.75}$$

$$\bullet \langle \kappa^2(\theta) \rangle = \langle \gamma^2(\theta) \rangle$$

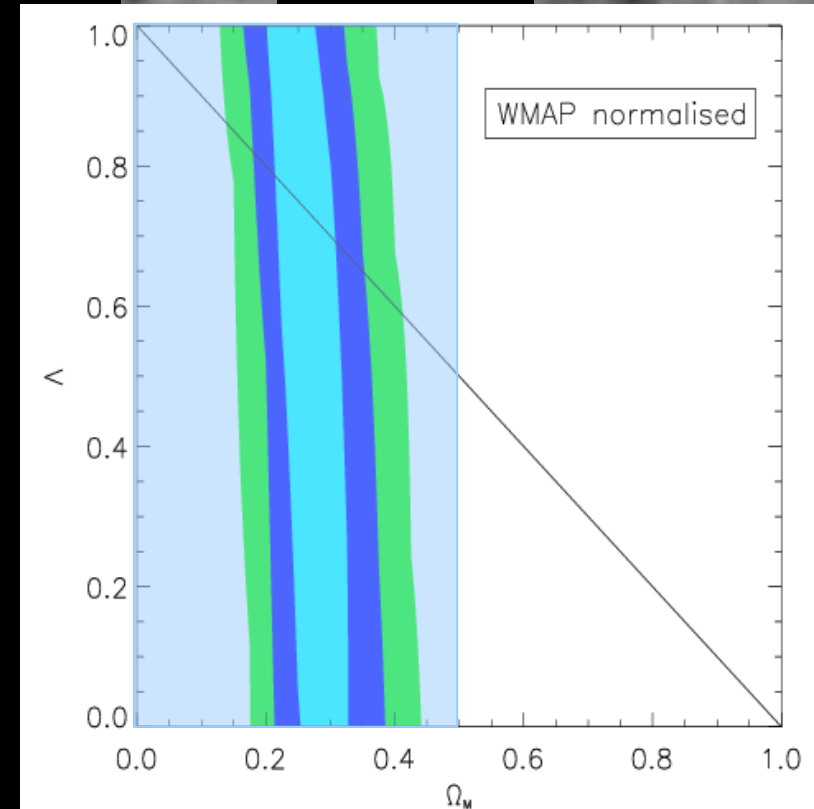
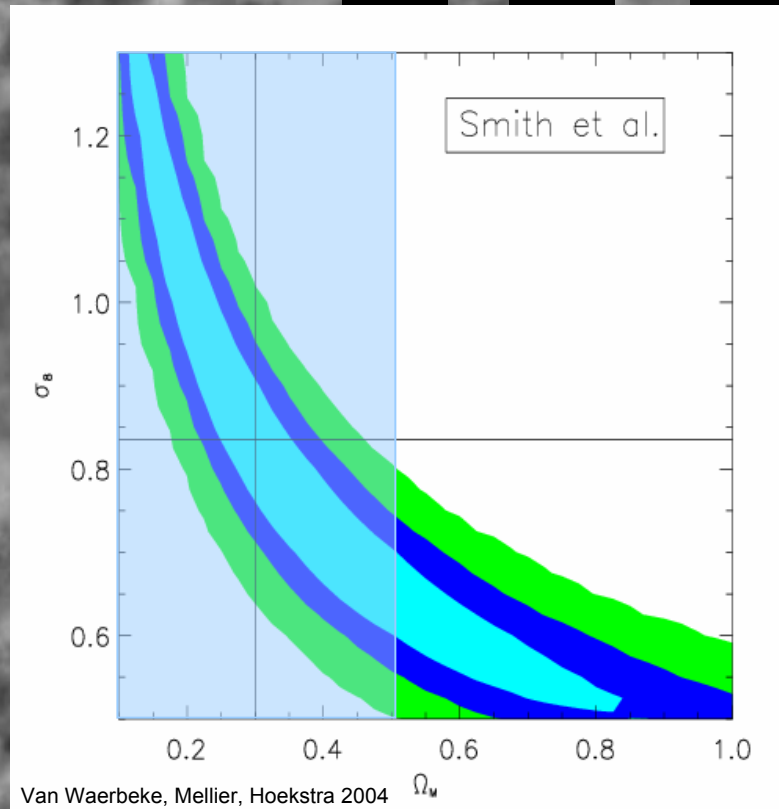
$$\bullet S_3(\kappa) \approx 40 \Omega^{-0.8} z_s^{-1.35}$$

Bernardeau, van Waerbeke, Mellier 1997,
Jain & Seljak 1997
Need mass maps for skewness

- Distribution increasingly skewed by gravity that will produce non-linear structures (clusters, groups, galaxies):
- $S_3(\kappa)$ will provide a statistical description of these non-linear systems



Breaking degeneracies with the skewness of the convergence

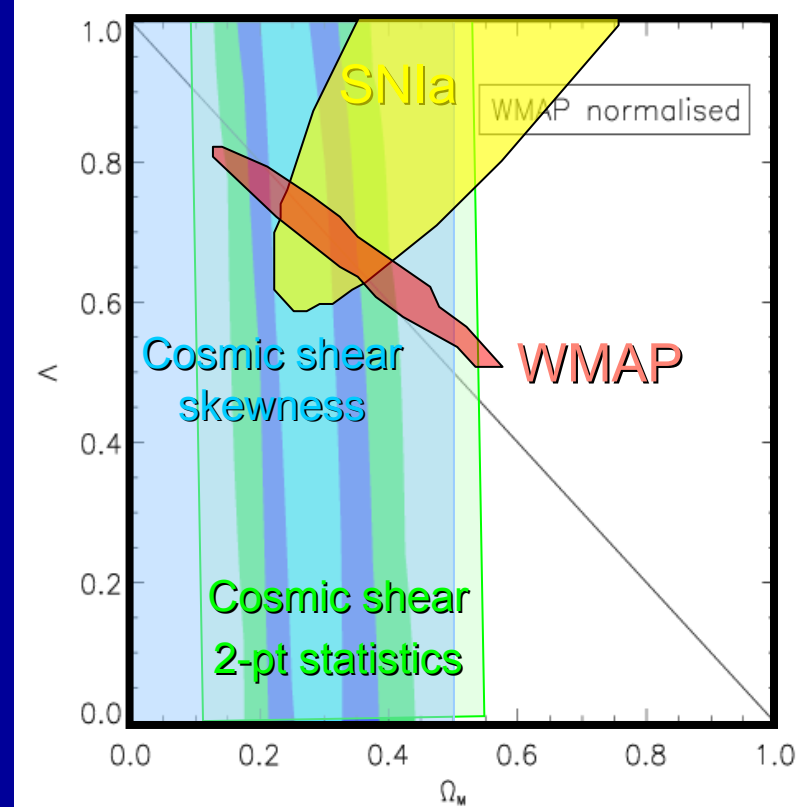
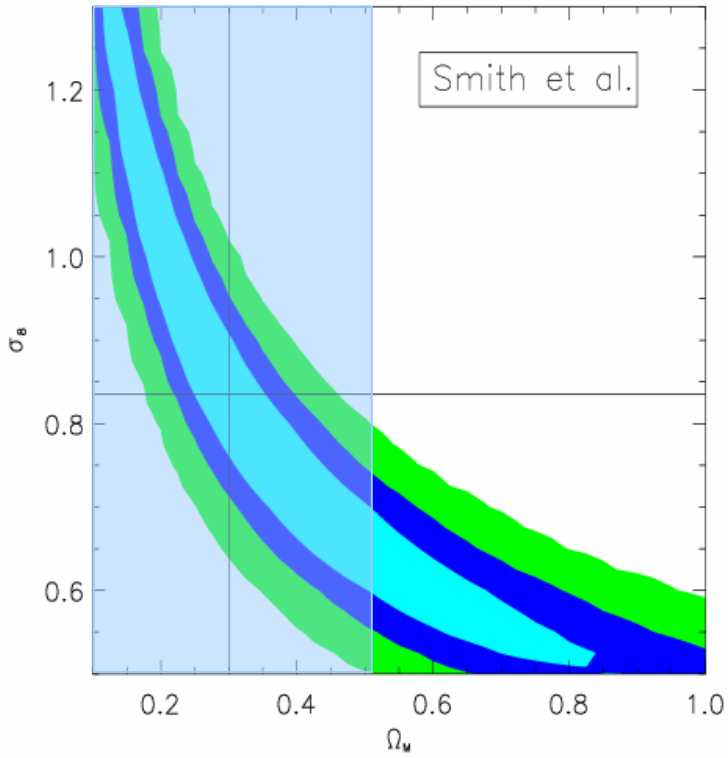


Uncertainties

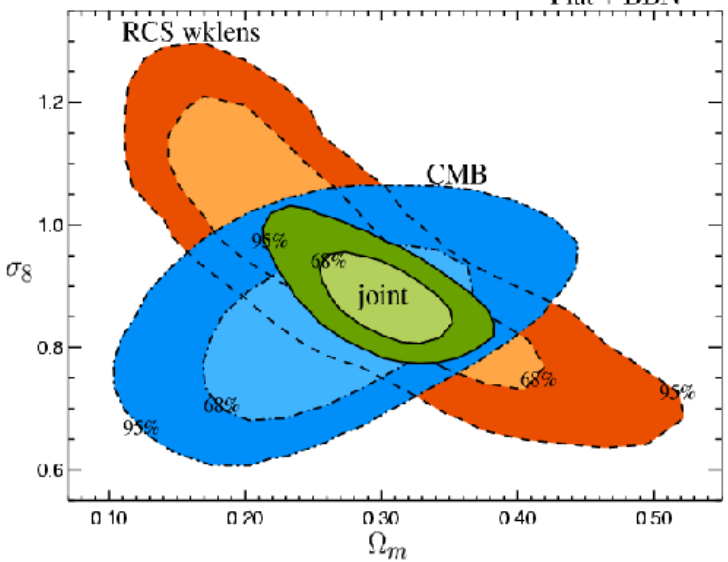
- Mass reconstruction in a Swiss cheese image
- $N(z)$ and source/lens clustering (Hamana et al 2000)

Joint analyses

Van Waerbeke et al 2004 + Pen et al 2003



Contaldi et al 2003



WMAP+CBI+New VIRMOs-Descart

(van Waerbeke, Mellier, Hoekstra, 2004)

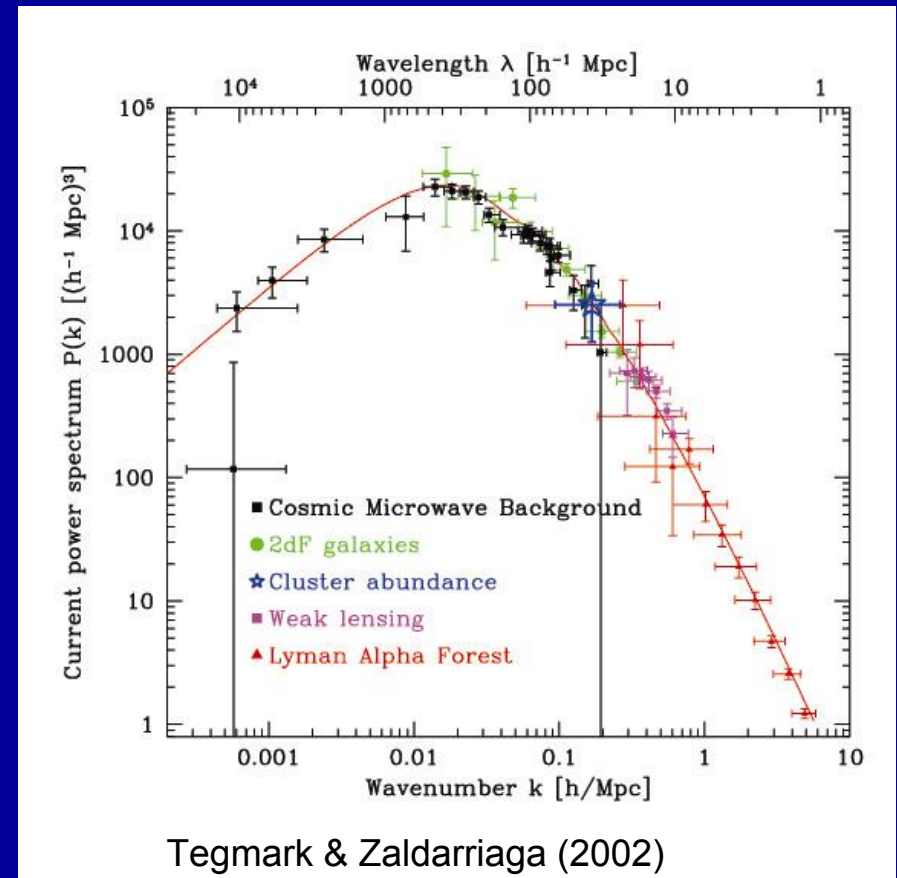
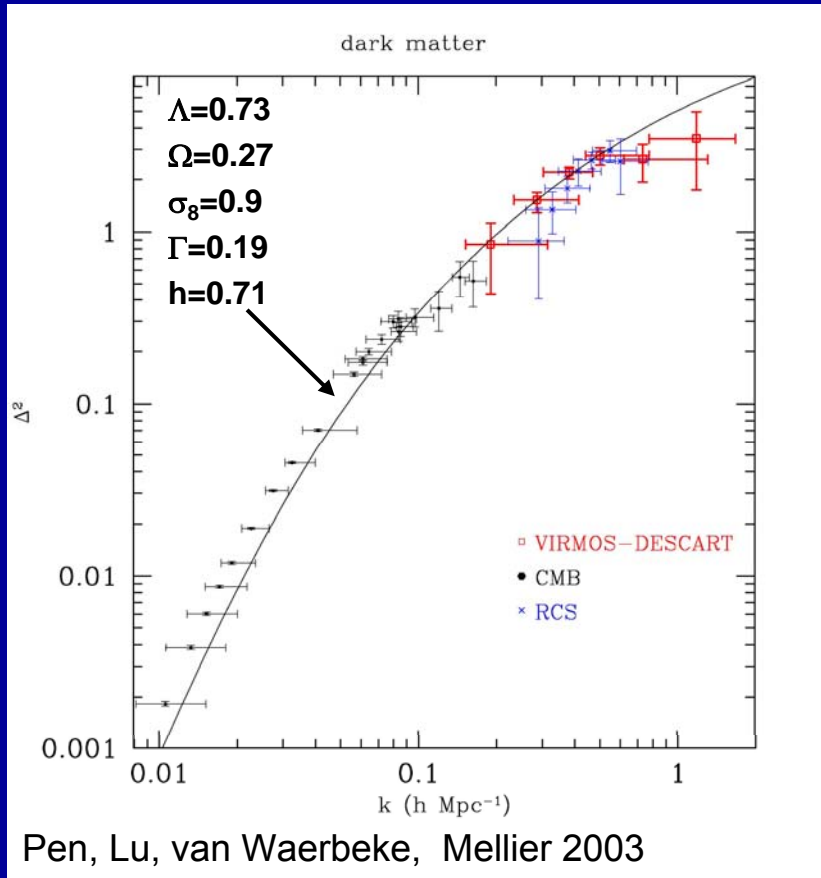
+ RCS (Hoekstra et al 2002) :

$$\sigma_8 = 0.85 \pm 0.06$$

$$\Omega_m = 0.30 \pm 0.07$$

3D dark matter reconstruction

3D inversion from 2D spectra (galaxies & DM), using broad bands estimates (M_{ap})



Still in a early phase, but

- Very promising for next generation surveys
- Evolution with photo-z +spectro-z likely feasible

(see also, Heavens 2003, Taylor et al 2003)

Biassing : Galaxy light vs. (dark) matter

Characterization of the relation between galaxies and matter?

- Mean biasing ($\langle n \rangle = b \cdot \langle \delta \rangle$)
- Deviation to linearity
- Scatter
- Time evolution

Schneider 1998, van Waerbeke 1998

$$\langle N_g M_{ap} \rangle / \sqrt{\langle N_g^2 \rangle \cdot \langle M_{ap}^2 \rangle} = f_1(\Omega_m; \Lambda) \cdot r$$
$$\langle M_{ap}^2 \rangle / \langle N_g^2 \rangle = f_2(\Omega_m; \Lambda) \cdot [\Omega_m / b]^2$$

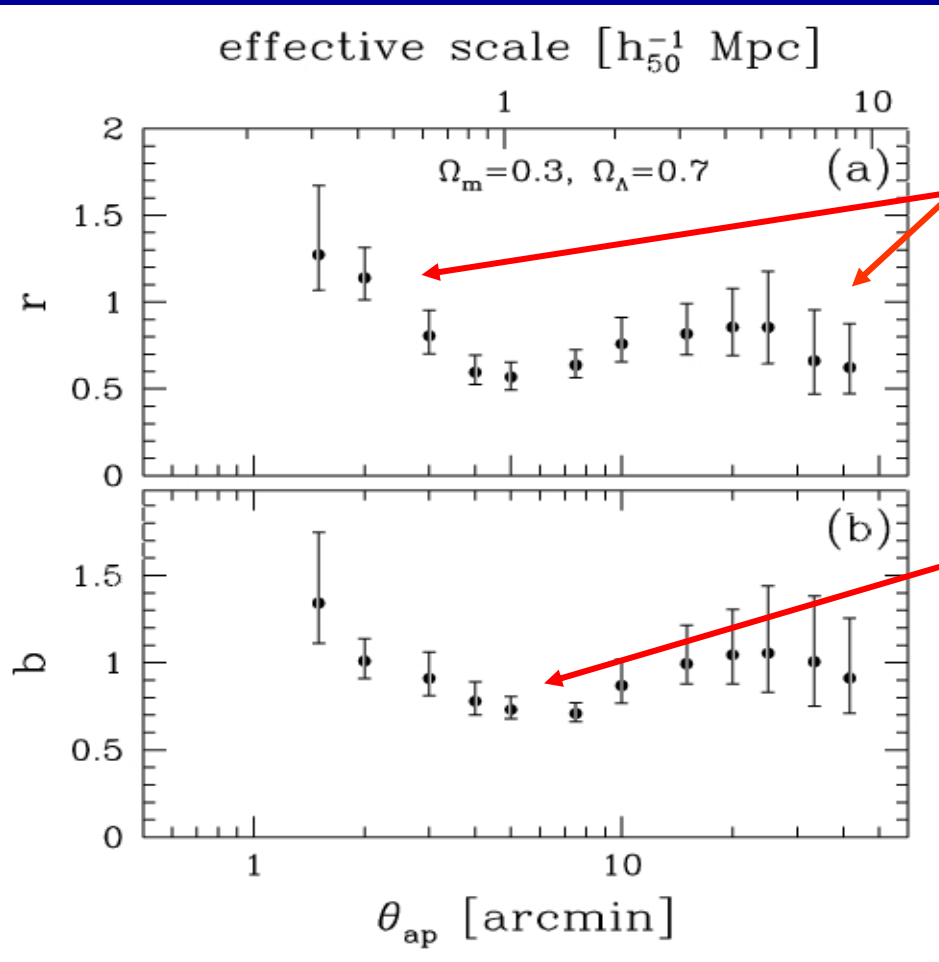
Foreground

If and only if linear and deterministic biasing:: $r=1$

- Linear + deterministic biasing : $r=1$; $\langle n \rangle = b \cdot \langle \delta \rangle$
- Non linear + deterministic: $1/r$
- Linear + Stochastics: $\sigma_b = b \cdot (1-r^2)^{1/2}$

VIRMOS-DESCART+RSC: Total : 11 + 40 deg²

Hoekstra, van Waerbeke, Yee, Mellier, Gladders 2002



$r = 1$: good correlation between mass and light on small scales...
Luminous galaxies are surrounded by massive halos.

$b = 0.7$: matter more strongly clustered than galaxies

- Strength : direct measurement of biasing, mass/DM correlation
- Weakness: non-linearity/ stochasticity degeneracy;
hard to interpret without high res. simulations

Cosmic shear and cosmology

GOOD:

- $f(z_l, z_s, \Omega_k, \Omega_b, \Omega_v, \Omega_\gamma, \Omega_{\text{CDM}}, \Omega_X, \Omega_\Lambda)$: cosmological parameters
- $P(k, z)$:
 - amplitude, shape, distortion, evolution;
 - direct description of the non-linear matter power spectrum;
 - halos properties (mass, profile, typical scale) : galaxies (galaxy-galaxy lensing), clusters of galaxies (mass maps; strong+weak lensing)
- Mass and light: properties of biasing as function of scale and *redshift*
- Poisson equation: test of gravity properties far beyond solar system scale
- B-mode analysis can be used to estimate systematic residual (non lensing signal)

BAD:

- Very weak signal on large scale: measuring very small changes in galaxy ellipticity is technically challenging (systematic residuals critical)
- Degeneracies: geometry x power spectrum
- Sensitive to redshift distribution of lenses/sources
- Signal higher on small scales, but non linear DM power spectrum unknown
- Contaminated by intrinsic correlation of ellipticities

Errors in σ_8

Ellipticity badly measured
(PSF anisotropy corrections,
shape measurement)

Redshift of sources badly
estimated (photo-z, too
deep for spectroscopy)

$$\langle e^2 \rangle = \langle \gamma^2 \rangle \sim 0.01 \quad \sigma_8^2 \Omega^{1.6} z_s^{1.4} \theta^{-(n+2)/2}$$

Shear is contaminated by
non-lensing signal (intrinsic
alignment of galaxies)

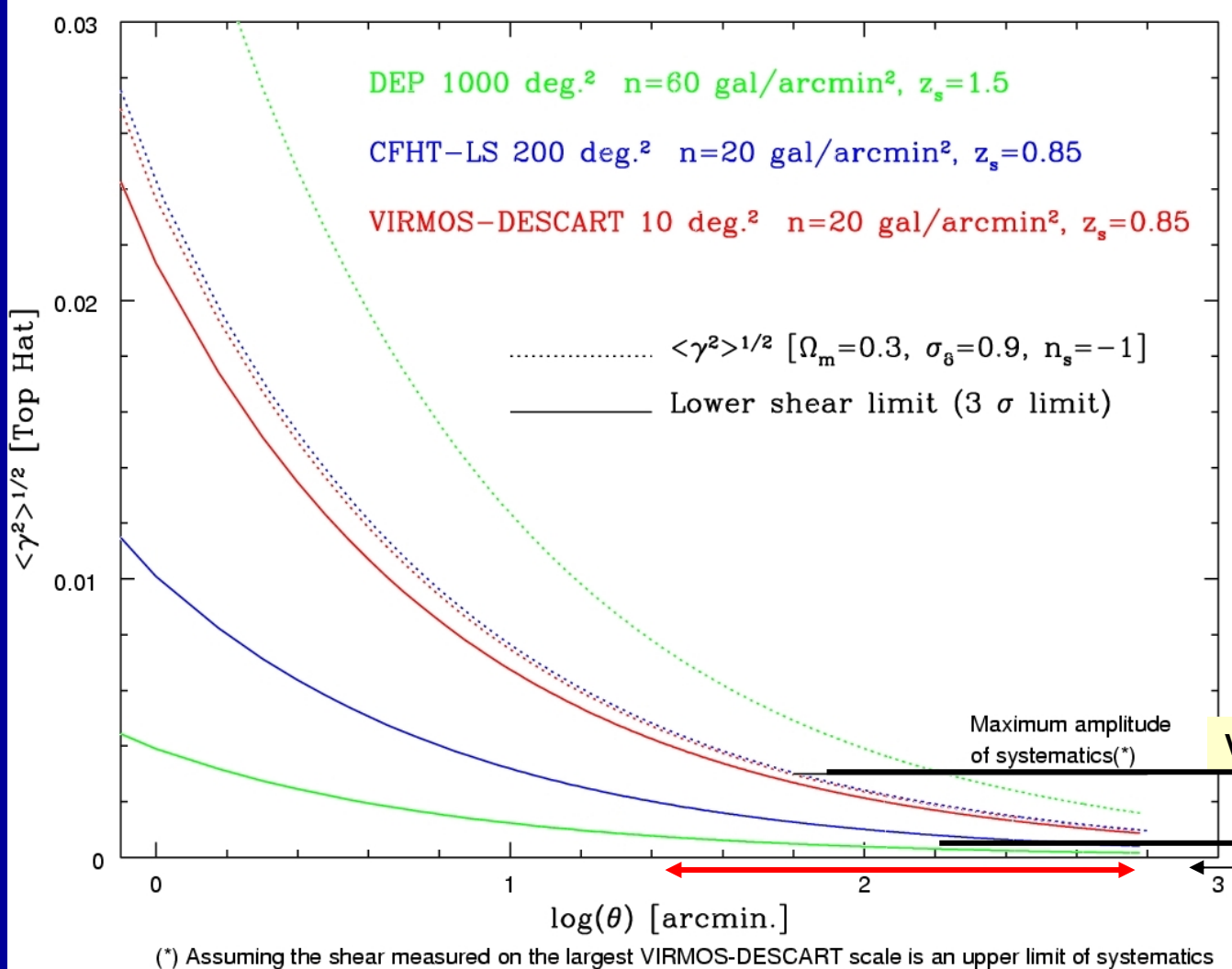
Non-linear evolution of dark matter
power spectrum unknown,
extrapolation on small scales wrong

Most critical: PSF anisotropy correction (B-mode analysis) + redshift of sources

The next challenges

- Dark matter power spectrum:
 - On larger scales (linear regime)
 - With better accuracy
 - As function of z
- Biasing of galaxies:
 - As function of scales
 - As function of local density/environment
 - As function of redshift
- New specifications
 - Poisson noise: depth
 - Multi-lens plane: depth, good z
 - Larger sky coverage
 - Better shape measurements: better image quality
 - Full B-mode suppression

Expectations from cosmic shear surveys



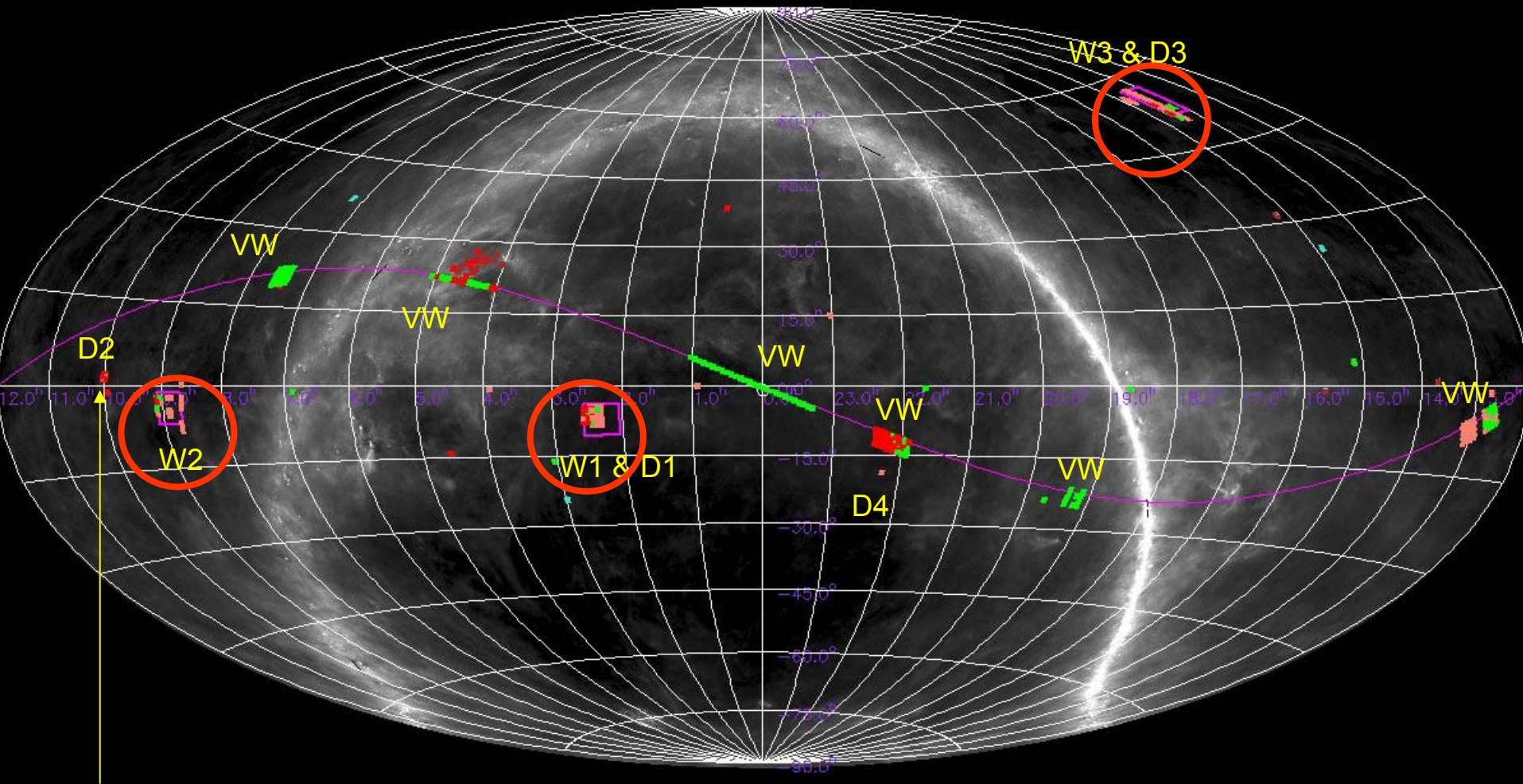
$$\langle \gamma(\theta)^2 \rangle^{1/2}_{limit} = 1.2\% \left[\frac{A_T}{1 \text{ deg}^2} \right]^{-\frac{1}{4}} \times \left[\frac{\sigma_{\epsilon_{gal}}}{0.4} \right] \times \left[\frac{n}{20 \text{ gal/arcmin}^2} \right]^{-\frac{1}{2}} \times \left[\frac{\theta}{10'} \right]^{-\frac{1}{2}}$$

$$\langle \gamma(\theta)^2 \rangle^{1/2} \approx 1\% \sigma_8 \Omega_m^{0.75} z_s^{0.8} \left(\frac{\theta}{10'} \right)^{-\left(\frac{n+2}{2}\right)}$$

Canada-France-Hawaii Telescope Legacy Survey: Canada-France collaboration

3 fields of 50 deg² , 4 deep fields of 1 deg²:

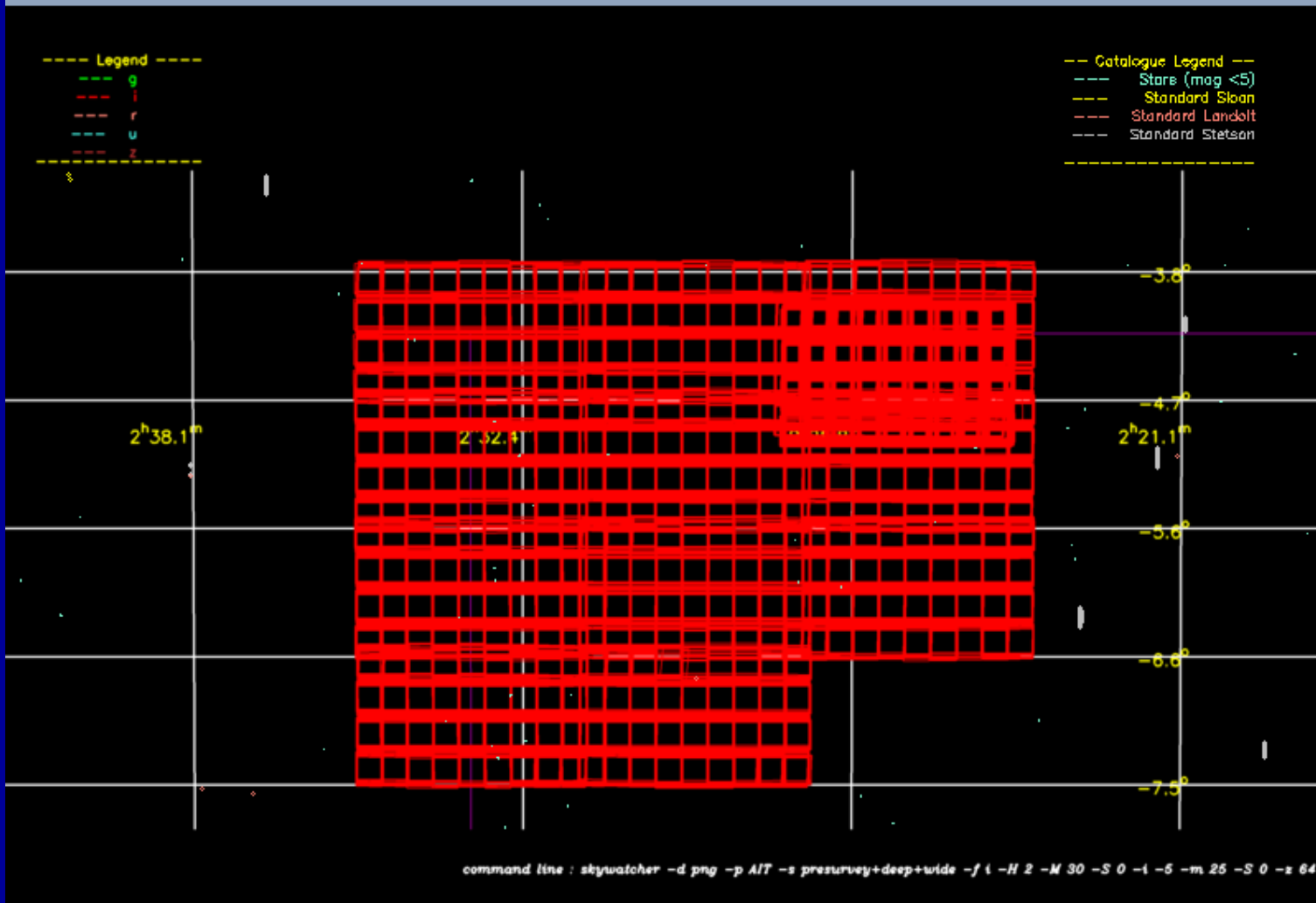
Total FOV 10 times present data sets; much larger angular scale probed



Cosmos

CFHTLS : Wide1 and Deep1 fields in I-band

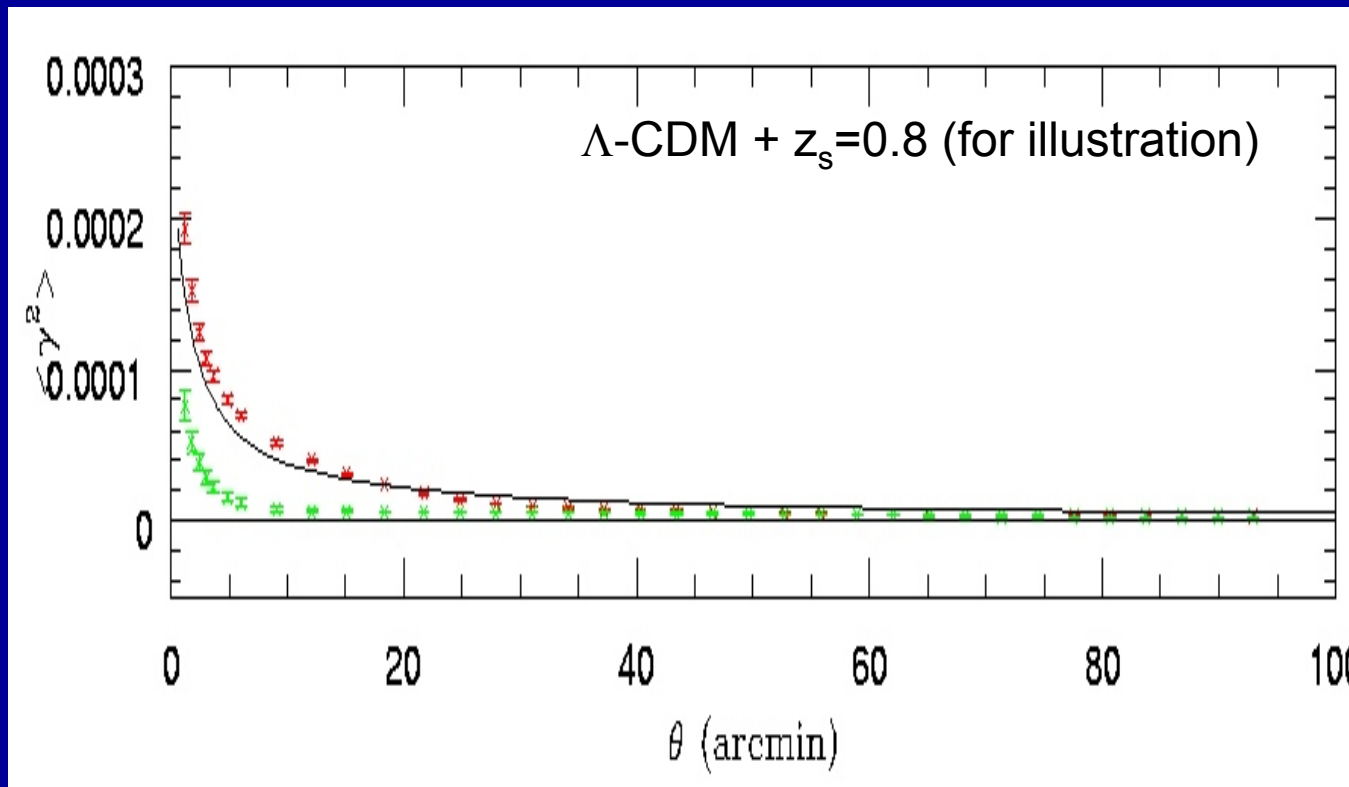
Terapix: Skywatcher



First exploration of cosmic shear on CFHTLS Wide

CFHTLS-W1 :

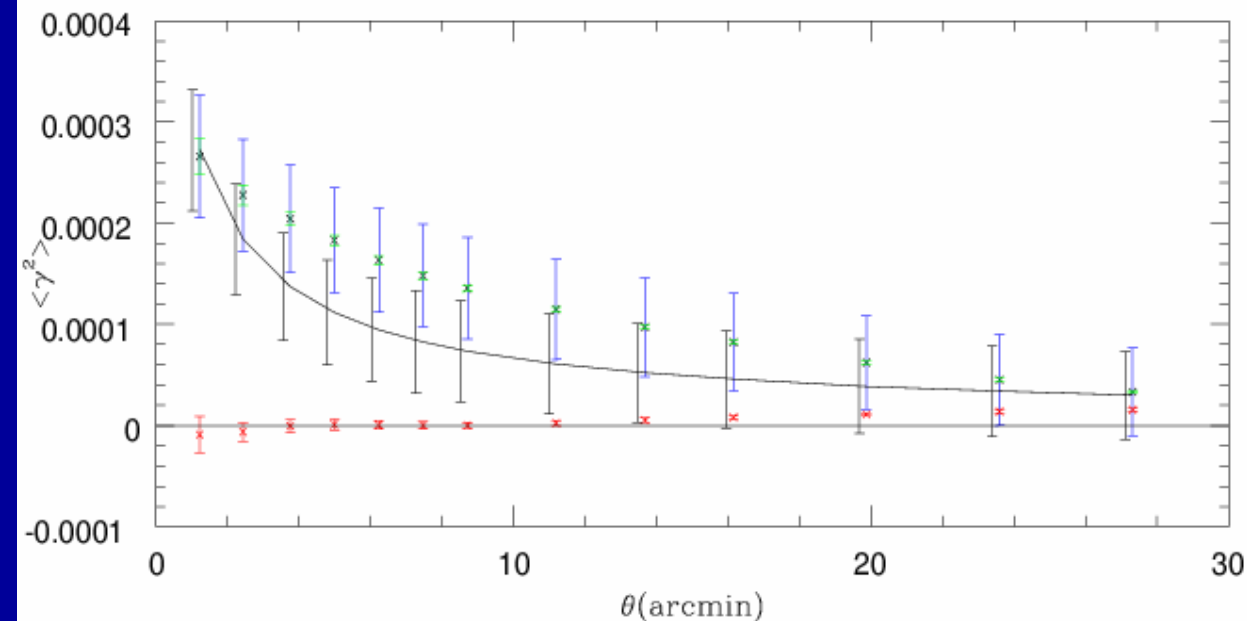
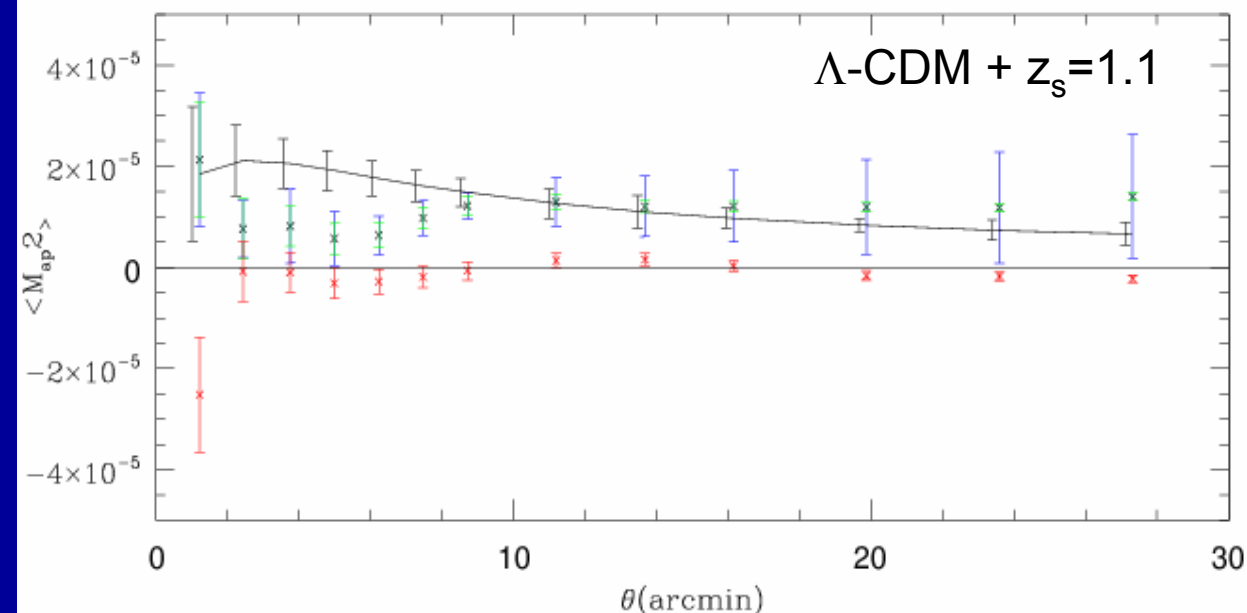
- shear variance i-band, 11 deg²
- Preliminary: data still in evaluation phase
- No-B modes at larger scales (most interesting)



The CFHTLS cosmic shear collaboration: Semboloni, Hoekstra, van Waerbeke, Mellier, Tereno, et al...

CFHTLS Deep field D1 from Terapix:

preliminary
estimates for
quality assessments



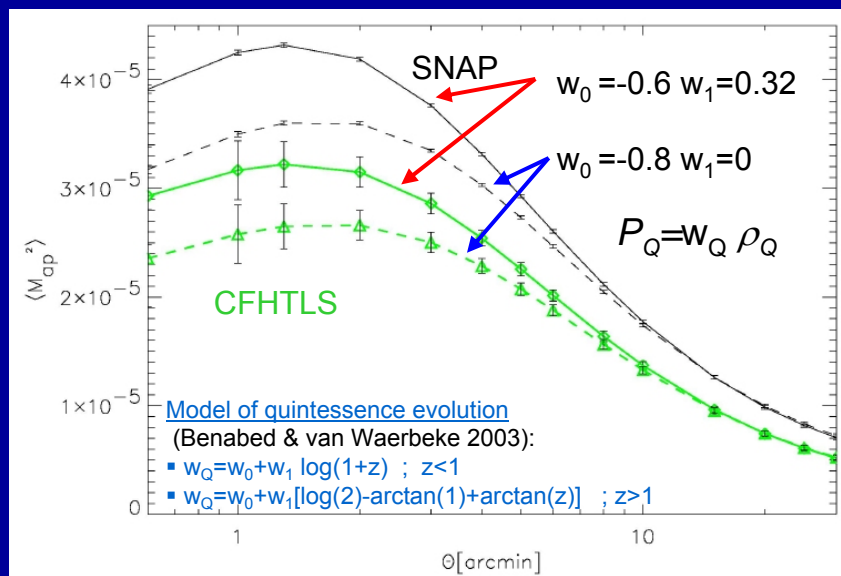
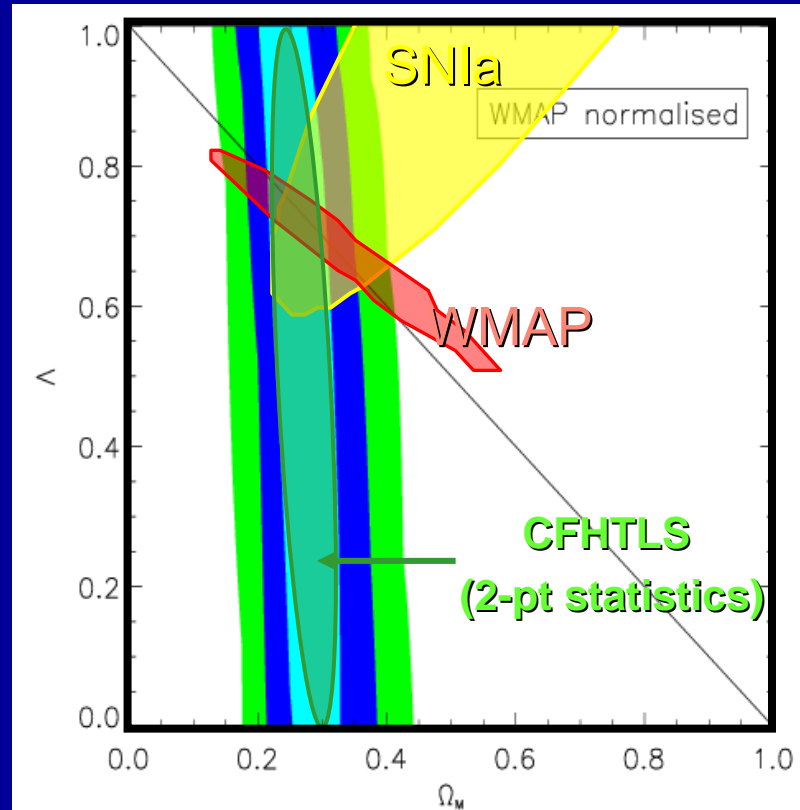
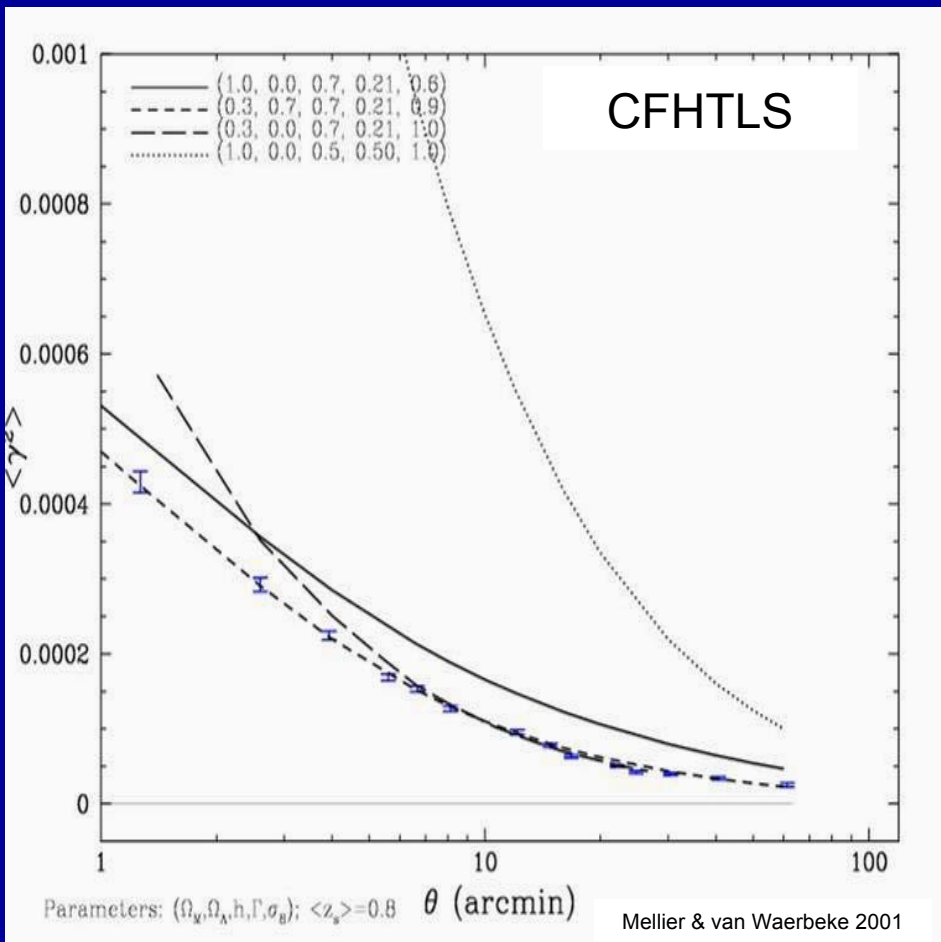
Good: Amplitude ratio
between CFHTLS D1 and
Virgos-Descart agrees with
expectations from depth ratio
(source redshift ratio)

D1 = deg² dominated by
cosmic variance

The CFHTLS cosmic shear
collaboration: Hoekstra,
Semboloni, van Waerbeke,
Mellier, Tereno, et al...

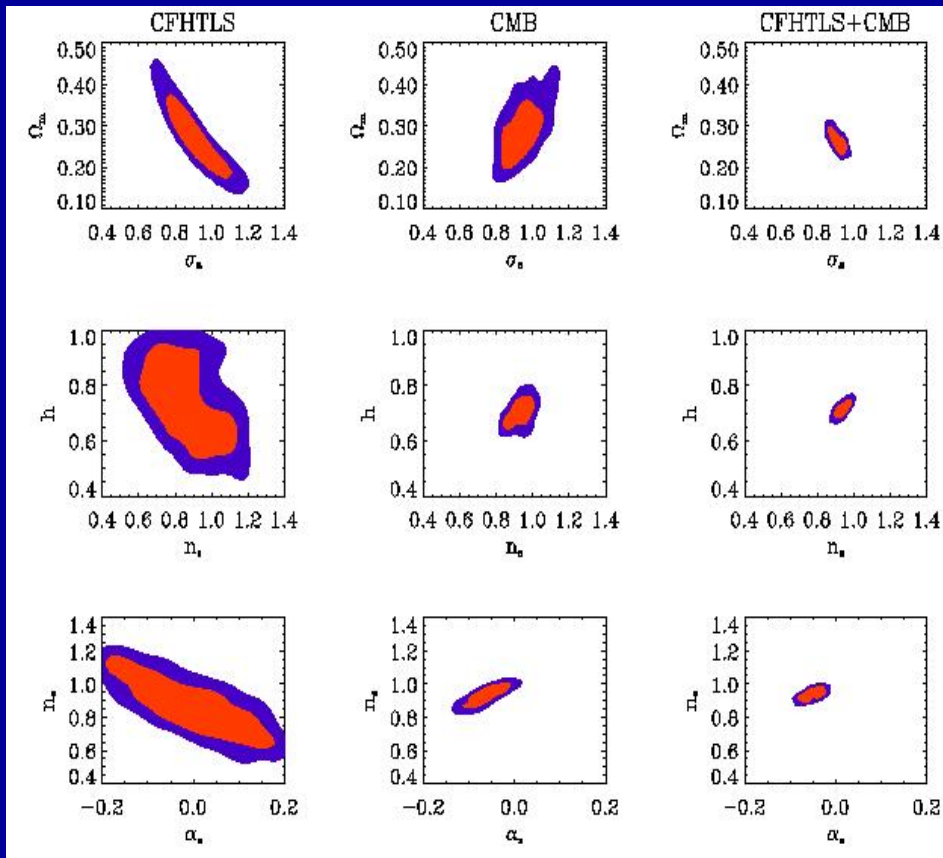
CFHTLS

goals in view of preliminary data



Cosmic shear CFHTLS + CMB

7 parameters MCMC ($\omega_b, \omega_c, h, n_s, \alpha_s, A_s, \tau$) : **CMB** (WMAP + CBI) and **Cosmic shear + CMB** (flatness imposed)



	gain
ω_b	1.4
ω_c	3.6
h	1.9
n_s	1.7
α_s	1.7
σ_8	2.5
Ω_m	2.8

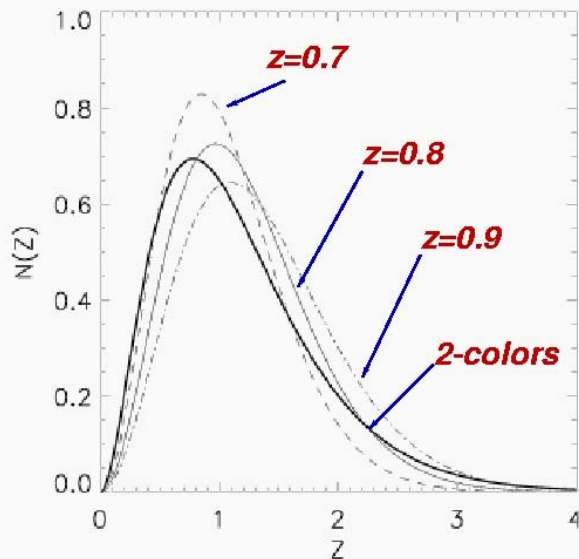
gain = $1\sigma(\text{CMB}) / 1\sigma(\text{cosmic shear}+\text{CMB})$

(see also Ishak et al 2004, which does a 1d joint cosmic shear + CMB forecast)

Redshift distribution:
a crucial issue for next
generation surveys

Sensitivity to redshift of sources

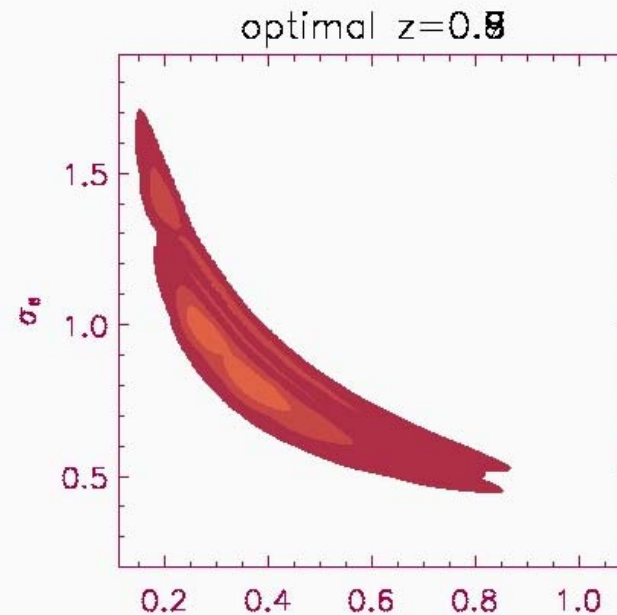
Redshift distribution of sheared sources



$$n(z_s) = \frac{\beta}{z_0 \Gamma\left(\frac{1+\alpha}{\beta}\right)} \left(\frac{z_s}{z_0}\right)^\alpha \exp\left[-\left(\frac{z_s}{z_0}\right)^\beta\right]$$

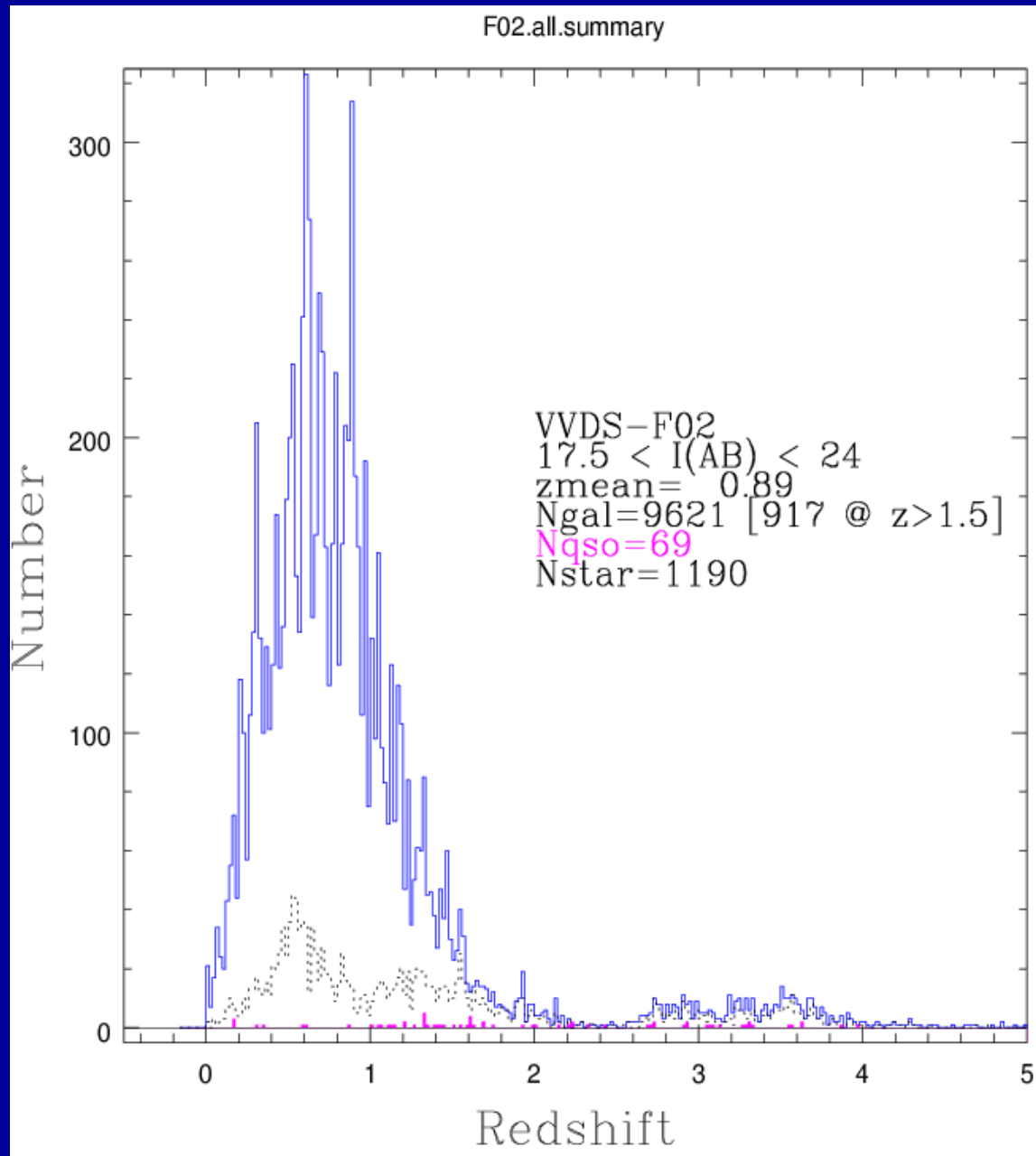
van Waerbeke et al 2001

VIRMOS-DESCART CFH survey



6.5 deg² - 450,000 galaxies - l=24

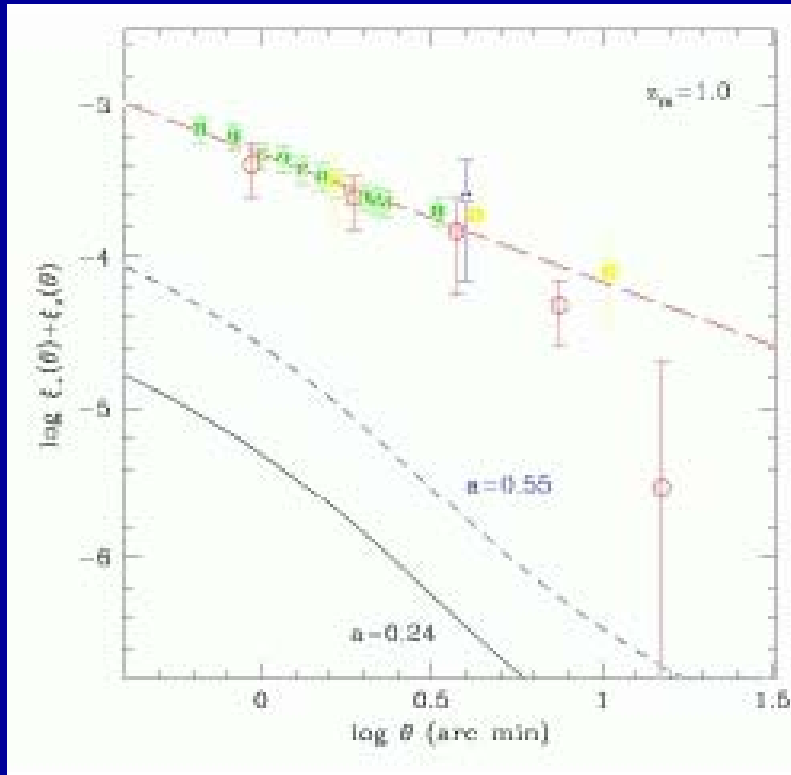
$z_s = 0.7+08+09$ - Open CDM - $\Lambda=0$, $\Gamma=0.21$



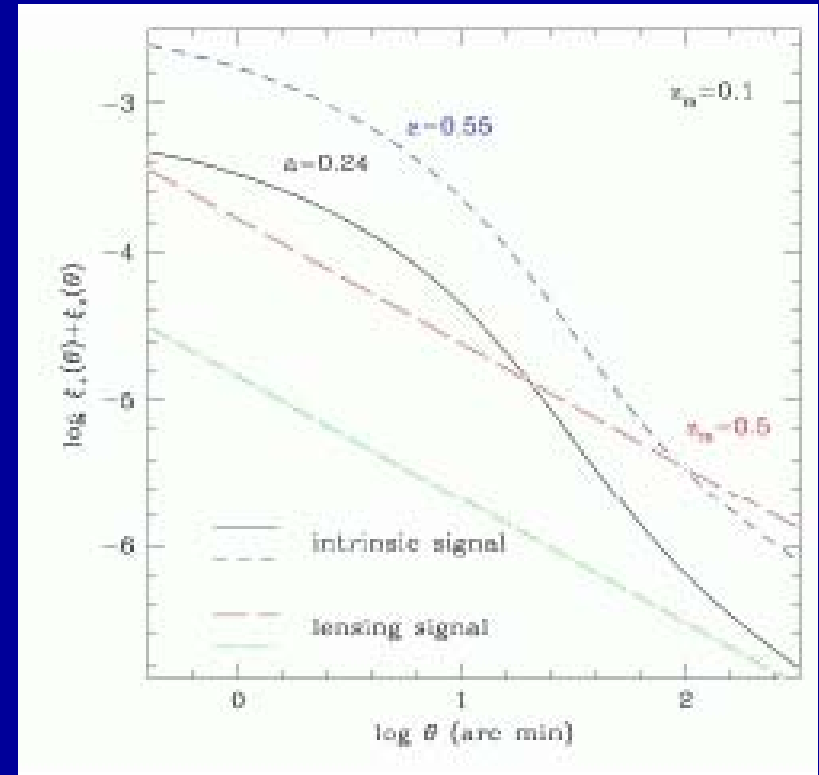
The VIRMOS-VVDS spectroscopic survey

Le Fèvre et al 2004

Intrinsic ellipticities: critical for low- z surveys



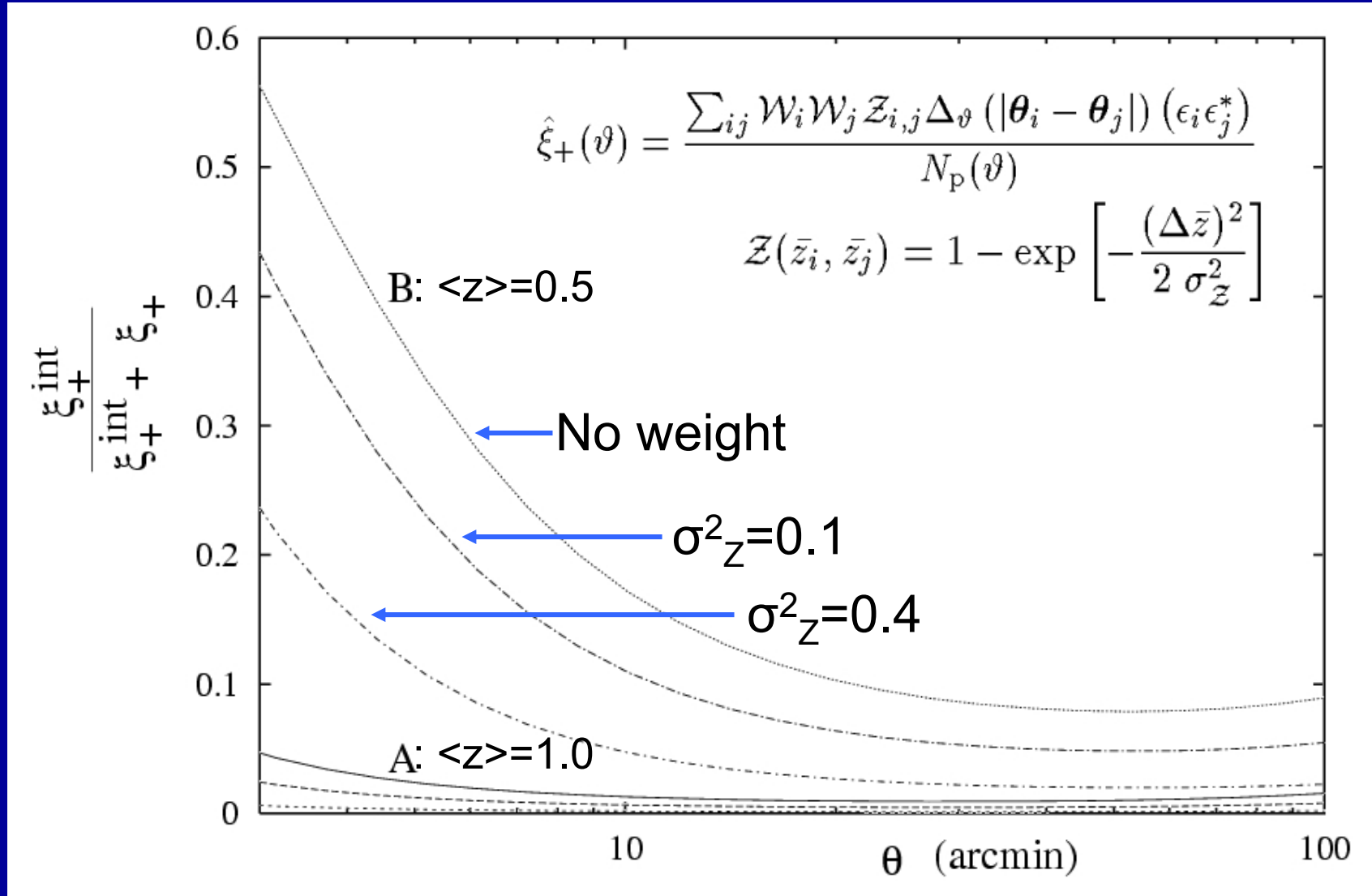
Crittenden et al 2001



See also : Mackey et al 2001; Catelan et al 2001; Croft & White 2001...

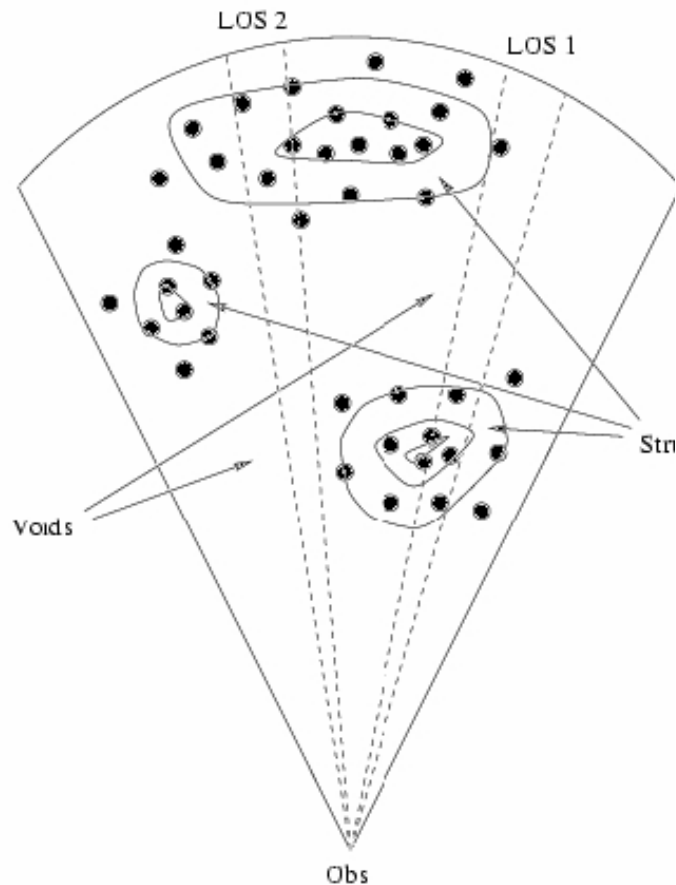
Minimising intrinsic alignments with photo-z

King & Schneider 2002 (see also Heymans & Heavens 2002)

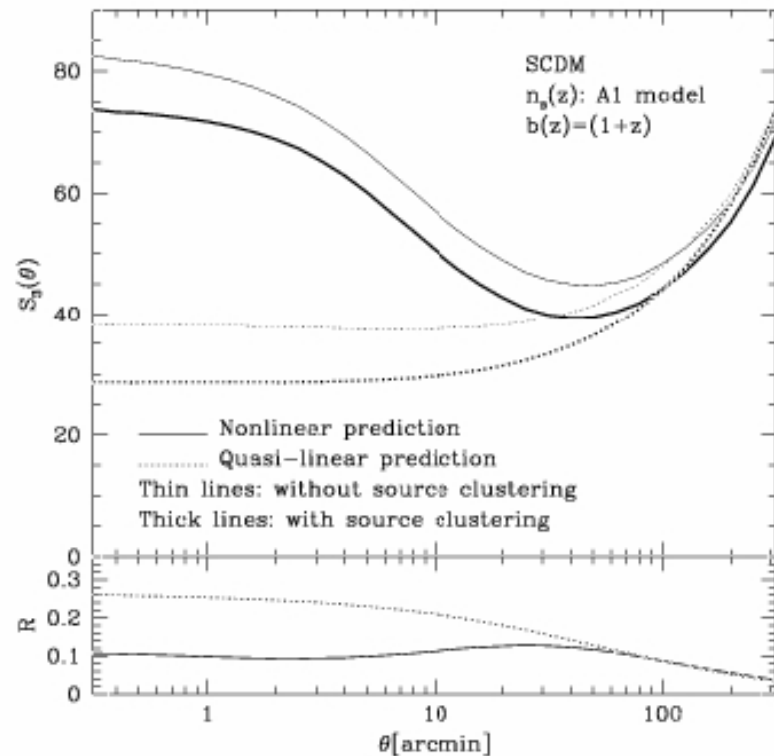


Impact of source clustering

Hamana et al 2000



Hamana et al 2000



$$R = S_3^{SC} / S_3$$

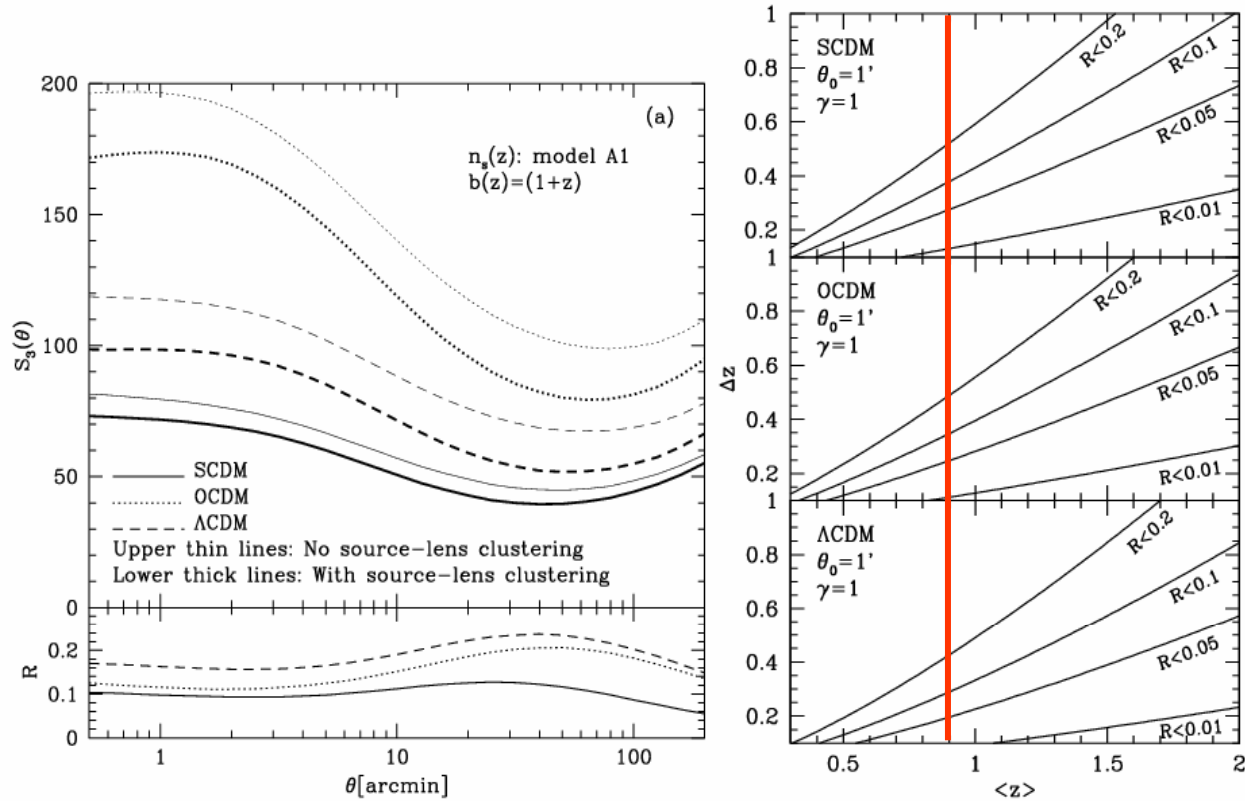


Figure 4. Sensitivity of the convergence skewness to source-lens clustering. The top-left panel shows how the amplitude of the skewness varies with source-lens clustering for three cosmological models. The lower plot gives the relative variation. In all cases, the skewness decreases by a factor larger than 10%, a serious limitation to precision cosmology with cosmic shear. To solve this issue, one needs to get the redshift of source-lenses. On the right panel, the width of the source distribution is plotted as function of the averaged source-redshift. In order to minimize the clustering effect, the source distances must be large as possible and spread over a narrow redshift range. Clearly, the accuracy of photometric redshift must be better than 10%. This goal can be achieved if *UBVRIJ* and *JHK* band data are obtained for most lensed galaxies, with a photometric accuracy of about 5%-10% in each filter.

Decoupling geometry and matter power spectrum

$$P_{g\gamma}(\ell; f, b) = \frac{3\Omega_{m0}H_0^2}{2c^2} \int \frac{d\chi_r}{a(\chi_r)} W_f(\chi_r) \int d\chi_b W_b(\chi_b) \times \frac{\chi_b - \chi_r}{\chi_b \chi_r} P_{g\delta}(\frac{\ell}{\chi_r}, \chi_r) \Theta(\chi_b - \chi_r) \quad (2)$$

$$P_{\gamma\gamma}(\ell; f, b) = \left(\frac{3\Omega_{m0}H_0^2}{2c^2} \right)^2 \times \int d\chi_r W_f(\chi_r) \int d\chi_b W_b(\chi_b) \times \int \frac{d\chi}{a(\chi)^2} \frac{\chi_b - \chi}{\chi_b} \frac{\chi_r - \chi}{\chi_r} P_{\delta\delta}(\frac{\ell}{\chi}, \chi) \Theta(\chi_b - \chi) \Theta(\chi_r - \chi). \quad (3)$$

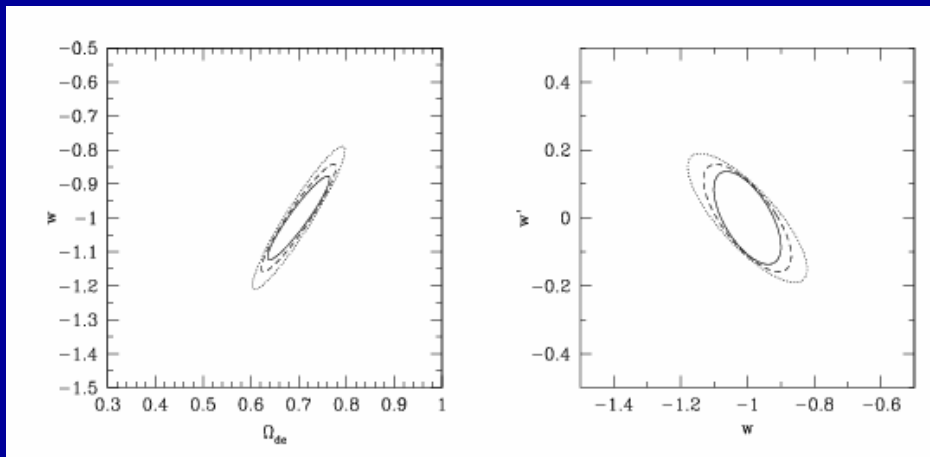
If small overlap between lensed populations :

$$P_{g\gamma}(\ell; f, b) \approx F(\ell; f) + G(\ell; f)/\chi_{\text{eff}}(b)$$

$$P_{\gamma\gamma}(\ell; f, b) \approx A(\ell; f) + B(\ell; f)/\chi_{\text{eff}}(b)$$

Signal can be scaled without regards on power spectrum: ratio only sensitive to geometry

$$\frac{P(\ell; f, b) - P(\ell; f, b')}{P(\ell; f, b'') - P(\ell; f, b''')} = \frac{\chi_{\text{eff}}(b)^{-1} - \chi_{\text{eff}}(b')^{-1}}{\chi_{\text{eff}}(b'')^{-1} - \chi_{\text{eff}}(b''')^{-1}}$$



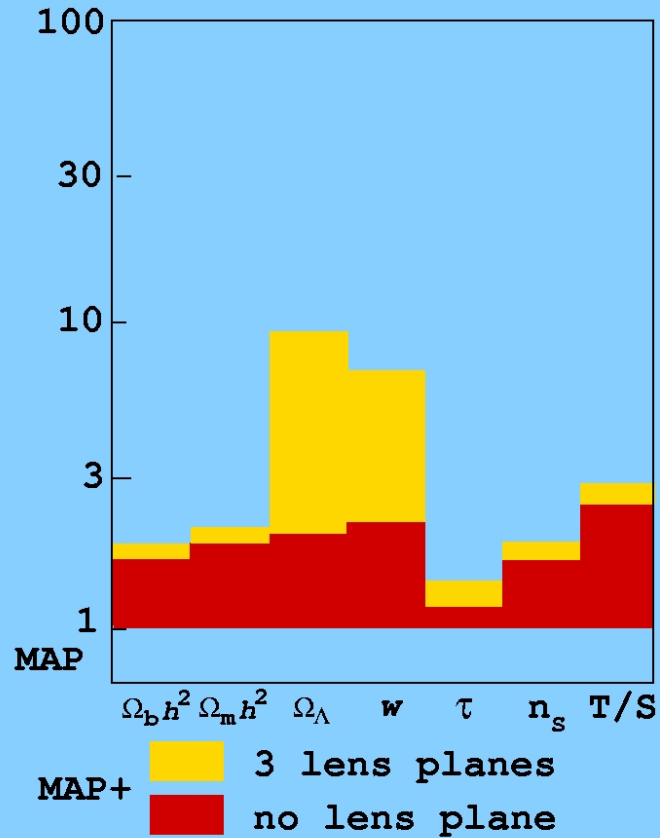
But need photo-z for at least 3 source planes

Zhang, Hui, Stebbins 2003:

4000 deg²

Error photo-z: 0.01, 0.02, 0.05

Error improvement : 25 deg²

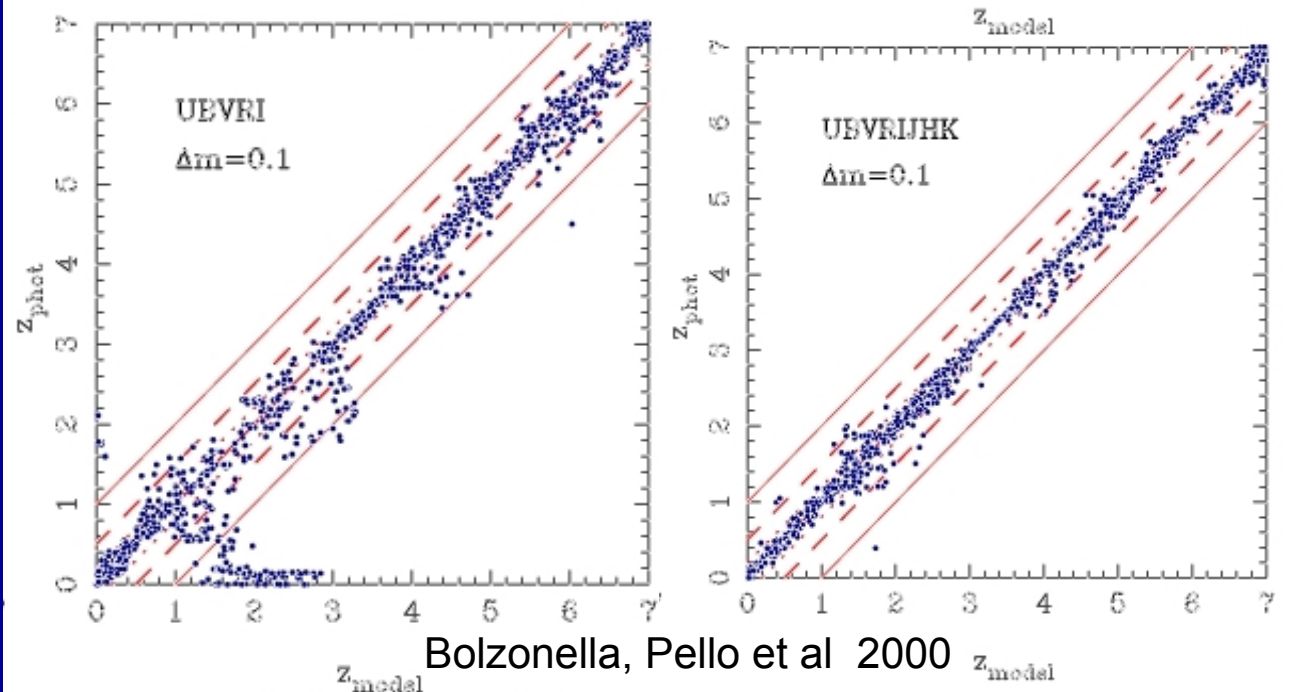


Breaking
degeneracies with
N(z)

CFHTLS (Megacam+Wircam): intermediate: 200 deg²

- It must be done in both visible and NIR... Another challenge!!

Need for redshift information



- Rough $N(z)$: $\Delta z = 0.05$
- Give a photo- z to all galaxies (weight galaxies for WL and intrinsic correlations of ellipticities): $\Delta z = 0.10$
- Provide multi-lens planes information dark energy: $\Delta z = 0.10$ sample 0.3/0.4/>0.5
- Partially constrain clustering: 3-pt function: $\Delta z = 0.05$
- Redshifts of arcs and lensing clusters: $\Delta z = 0.10$
- Break power spectrum / geometry: $\Delta z = 0.05$
- Biasing background / foreground: $\Delta z = 0.10$ foreground $z < 0.2$
- Biasing as function of redshift: 3 planes: $\Delta z = 0.10$ sample: 0.2/0.4/>0.5

Wircam and cosmic shear with CFHTLS

- Ideal: Photo-z informations for all galaxies used for weak lensing :
- $I_{ab}=24$.: extended object 5σ , 80% completeness of the I-band sample: J=22.8 (1hr), H=21.8 (1hr), K=21.3 (1hr) .
- FOV Megacam/Wircam: R= 9
- Covering the W1 field : $Ct=time*1.2$ (overlap between fields) :
72 (W1) x 9 (R) x 3 (filter)*1.2 (Ct) = 2333 hrs, 360 nights (65% efficiency)
- Covering the 3 Wide fields: 850 nights
- Redshift survey cannot provide all z, but must be used to calibrate photo-z and errors/systematic
- Suggestion:
 - 30% of W1 (110 nights) + 30% W3 (cosmic variance)
 - Or 30% $I=24$ W1 + 70% $I=22.5$ W1 (full W1)
- Cosmic shear also use Deep fields
- Priority to
 - Deep D1
 - Wide W1 and W3 (spectro z exist)

